

This document is the accepted manuscript version of the following article:
Garg, D. K., Serra, C. A., Hoarau, Y., Parida, D., Bouquey, M., & Muller, R. (2020). Numerical investigations of perfectly mixed condition at the inlet of free radical polymerization tubular microreactors of different geometries. *Macromolecular Theory and Simulations*. <https://doi.org/10.1002/mats.202000030>

DOI: 10.1002/marc.((insert number)) ((or ppap., mabi., macp., mame., mren., mats.))

Full Paper

Numerical investigations of perfectly mixed condition at the inlet of free radical polymerization tubular microreactors of different geometries

Dhiraj K. Garg*, Christophe A. Serra, Yannick Hoarau, Dambarudhar Parida, Michel Bouquey, Rene Muller

Dr. Dhiraj K. Garg

Shiv Nadar University, Dadri, Gautam Buddha Nagar, UP, India-201314

Email: dhiraj.garg@snu.edu.in

Prof. Christophe A. Serra

Université de Strasbourg, CNRS, ICS UPR 22, F-67000 Strasbourg, France

Email: serrac@unistra.fr

Prof. Yannick Hoarau

Université de Strasbourg, CNRS, ICUBE UMR 7357, F-67412 Illkirch, France

Email: hoarau@unistra.fr

Dr. Dambarudhar Parida,

Empa, St. Gallen, Lerchenfeldstrasse 5, 9014 St. Gallen, Switzerland

Email : dambarudhar.parida@empa.ch

Dr. Michel Bouquey, Prof. Rene Muller

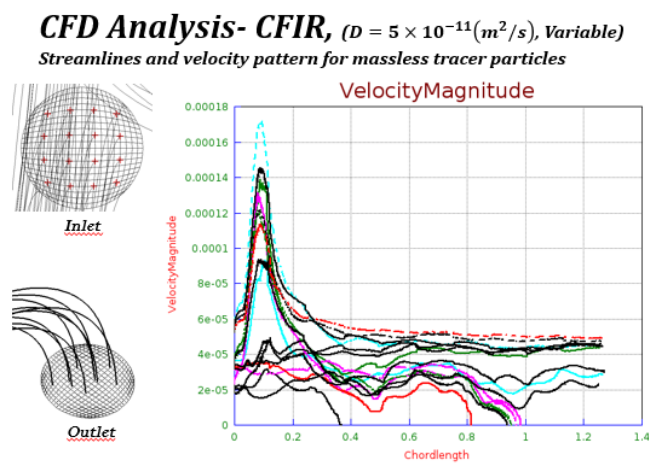
Université de Strasbourg, CNRS, ICS UPR 22, F-67000 Strasbourg, France

Email: michel.bouquey@unistra.fr, rene.muller@unistra.fr

The numerical investigation of free radical polymerization (FRP) of methyl methacrylate under mixed feed condition at inlet was made for three microtubular reactor geometries, namely straight tube (STR), coiled tube (CTR) and coil flow inverter reactor (CFIR). The effect of variation of fluid thermo-physical properties (FTPP) (density, viscosity and thermal conductivity) with reaction along with discrete variation of chemical species diffusion coefficient was studied. Predicted values of monomer conversion, number average chain length (DP_n) and polydispersity index (PDI) were found to be systematically lower for variable FTTP case compared to constant FTTP case. But contrary to expectations, results were found to be independent of reactor geometry for either case. Results clearly showed the importance of modeling the variation of FTTP especially with respect to conversion. One case of varying diffusion coefficient of each chemical species based on free volume theory with constant FTTP

was also simulated. Here again, the results were found to be independent of reactor geometry. Constant thermal conductivity and isothermal reactor condition were found to be good assumptions. This study clearly established the need not only for variable FTPP, thus coupling transport processes but also for incorporating varying diffusion coefficient along with conversion in modeling of FRP in microreactors for better predictions.

FIGURE FOR ToC_ABSTRACT



1. Introduction

1
2
3 Since mixing has a profound impact on polymerization and polymer product properties,^[1] the
4 study of the feed mixing conditions - completely mixed or completely unmixed feed at reactor
5 inlet, is important. In flow reactors, active or passive mixing methods^[2] are used for ensuring
6 continuous mixing along the flow. Active methods are energy intensive and require physical
7 devices. Passive methods, on the other hand, induce the mixing by creating variation in flow
8 profile through reactor geometry. They are thus less energy intensive and have little
9 maintenance due to absence of moving components. In microreactor, diffusion process
10 contributes significantly to mixing besides convection mixing^[3,4] which is otherwise
11 insignificant in macro-scale industrial reactors.^[5] Polymerization in microreactor is a difficult
12 process to carry out due to very large increase of viscosity with conversion. To keep it
13 manageable, non-reactive solvent is generally added to dilute the reacting solution.

14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30 Computational fluid dynamics (CFD) can be used judiciously to study, evaluate and compare
31 various microreactor geometries and to choose the best among them and then optimize it but
32 this requires good mathematical modeling of polymerization. A mathematical model is being
33 judged for its goodness by its predictions compared to experimental data under similar
34 operating conditions. The question that how much comprehensive a mathematical model should
35 be, without becoming unnecessarily complex and computationally expensive to give acceptable
36 predictions, is really difficult. Some researchers^[4] modelled fluid thermo-physical properties
37 (FTPP) as constant while other^[5] had modelled the variation of FTTP during polymerization
38 simulation while all of them kept diffusion coefficient of various chemical species constant.
39
40
41
42
43
44
45
46
47
48
49
50
51
52 Keeping diffusion coefficient constant in modelling of polymerization is good when radial
53 Peclet number is high (>100) as generally is the case with industrial scale reactors of larger
54 dia.^[5] The same is not true for the case of microreactor, especially during lower conversions,
55 where the radial Peclet number could be low (<100). Low Peclet number implies that radial
56
57
58
59
60
61
62
63
64
65

1 diffusion is significant and must be accounted for while predicting mixing. Thus, modelling
2 continuous variation of diffusion coefficient seems to be necessary to evaluate mixing during
3 polymerization inside microreactors.
4

5 This leads to another two possibilities of modelling polymerization in microreactors –
6 modelling constant or variable FTTP alongwith continuous variation of diffusion coefficient
7 with conversion. Thus, there are four possibilities in all for modelling polymerization in any
8 microreactor- constant or varying diffusion coefficient in combination with constant or variable
9 FTTP. Each possibility requires different amount of computational resources based on
10 complexity of modelling. The modelling with constant diffusion coefficient would require
11 multiple simulations with different values of diffusion coefficient whereas with varying
12 diffusion coefficient, only one simulation is enough. This study actually looks into this issue
13 for existing and proposed improved modeling of free radical polymerization in tubular
14 microreactors under mixed feed conditions at reactor inlet.
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30

31 The effect of unmixed feed condition on free radical polymerization (FRP) in microreactors of
32 various geometries had already been investigated numerically by some researchers.^[3,4] They
33 had also compared those geometries for the mixing and polymer properties under unmixed feed
34 condition. They had done all their CFD modeling and simulation with the assumption of
35 constant FTTP during reaction. This assumption led to decouple the flow process from chemical
36 reaction, mixing and heat transfer. This shortcoming was removed to some extent in our
37 previous work.^[6] Two reactor geometries namely straight tube (STR) (**Figure 1(b)**) and coiled
38 flow inverter reactors (CFIR) (**Figure 1(f)**) were considered. The feed condition was
39 completely unmixed at reactor inlet. The processes were modeled along with variation of
40 density, viscosity and thermal conductivity as function of conversion and temperature (variable
41 FTTP). This coupled the flow process with heat transfer, mass transfer and chemical reactions
42 – conditions closer to reality. A new transformation (NT), developed in another work,^[7] was
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

1 used. The process conditions were still unmixed feed condition of FRP in straight tube (STR)
2 and coiled flow inverter (CFIR) tubular microreactors. This allowed feeding the CFD code for
3
4 FRP with data in molar form for chemicals species concentration and kinetic rates coefficients
5
6 instead of in mass form as used by other researchers.^[3,4] It was found that this approach reduced
7
8 numerical and modeling errors significantly and hence improved the predictions of FRP using
9
10 CFD in microreactors.
11

12 The simulations were carried out against the discrete variation of diffusion coefficient with its
13
14 value being same and constant for all the chemical species modeled. Its effect was observed on
15
16 several variables like monomer conversion X_M , polydispersity index (PDI) and number-average
17
18 polymer chain length (DP_n). The discrete variation was considered because of the difficulty to
19
20 model continuous variation of diffusion coefficient for each chemical species. Although this
21
22 approach was quite simplistic in nature, still it gave some understanding of the process inside
23
24 microreactor. Its effect was observed on several variables like monomer conversion X_M ,
25
26 polydispersity index (PDI) and number-average polymer chain length (DP_n) at reactor outlet.
27
28 Results were then compared with the constant FTTP modeling case under similar conditions.
29
30

31 Two reactor geometries namely straight tube (STR) and coiled flow inverter (CFIR) reactors
32
33 were considered. CFIR is a chaotic flow device (**Figure 1** (f)) which was found to significantly
34
35 increase internal mixing owing to 90° bends placed at regular intervals along the helix.^[8]
36
37 Significant differences were found in the prediction of X_M , DP_n and PDI after coupling the
38
39 processes compared to decoupled processes case of constant FTTP. Viscosity was found to rise
40
41 by about 6 orders from inlet to outlet and had profound impact on flow profiles in coupled
42
43 processes case. As a consequence, mixing due to convective flow was severely affected. An
44
45 anomalous case of increased convective mixing at low diffusion coefficient was observed which
46
47 could not otherwise be simulated and observed using constant FTTP. Thermal conductivity was
48
49 modeled as a function of X_M but no significant variation in its value was observed. The
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

1 temperature profile across cross-section of the microreactor was found to be uniform indicating
2 existence of isothermal condition even under the varying FPHP condition. CFIR was found to
3
4 perform better along with an improved control over polymer properties (lower *PDI*, higher
5
6 *DP_n*) compared to STR for unmixed feed under similar operating conditions. CFIR, a chaotic
7
8 flow device, was found to significantly increase internal mixing at industrial scale owing to 90°
9
10 bends placed at regular intervals along the helix.^[8] Here too, CFIR was found to perform better
11
12 along with an improved control over polymer properties (lower *PDI*, higher *DP_n*) compared to
13
14 STR under similar operating conditions for unmixed feed.
15
16

17
18 CFIR seemed to be a promising microreactor for FRP but required more thorough and rational
19
20 analysis of its performance against simpler and similar geometries. Besides this, completely
21
22 mixed feed condition at reactor inlet was general practice in labs and industry. So the current
23
24 study considered the case of mixed feed condition for the FRP of methyl methacrylate (MMA).
25
26 Three different tubular microreactor geometries were taken for current study. The flow was
27
28 taken to be laminar inside the microreactors. There was a gradual change in the geometry of
29
30 each microreactor for enhancing passive radial mixing.^[2] The first reactor geometry considered
31
32 was the straight tube (STR, **Figure 1 (b)**) which relied on radial mixing by mass diffusion only.
33
34 Second was the coiled tube reactor (CTR, **Figure 1 (d)**) which took benefit from secondary
35
36 flows arising from its curvature to increase radial mixing^[9-12] in addition to diffusion. The third
37
38 reactor geometry was the CFIR (**Figure 1 (f)**) which presented 90° bends in an helically based
39
40 geometry.
41
42
43
44
45
46
47

48
49 In current work, the improvement in mixing, control of polymer properties like *PDI* and *DP_n*
50
51 due to reactor geometry and coupling of various transport processes along with chemical
52
53 reaction were studied and evaluated in a more systematic way. For this, two different types of
54
55 modelling were used. For the first type of constant diffusion coefficient, like in our previous
56
57 work,^[6] two sets of simulations – one for coupled transport processes (through variable FPHP)
58
59
60
61
62
63
64
65

and another for decoupled transport processes cases (through constant FTPP) - were obtained for all the three microreactor geometries and results were then compared. This resulted in several simulations for different values of diffusion coefficient. For the second type of varying diffusion coefficient, for the first time, for all the three reactor geometries under same operating conditions, one simulation with modeling of continuous variation of diffusion coefficient for all chemical species of FRP using free volume theory^[13-15] was made while keeping FTPP constant. This was done to verify whether this would make the modeling sufficiently comprehensive, without becoming too complex and difficult to simulate, to give acceptable predictions.

1.1. Mathematical Model for CFD

Following equations were used for CFD problem with chemical reaction and heat effects:

The conservation of Mass (incompressible fluid)

$$\nabla \cdot u = 0 \quad (1)$$

The conservation of Momentum – Navier-Stokes equation

$$\rho \frac{\partial u}{\partial t} + \rho(u \cdot \nabla)u = -\nabla p + \nabla \cdot (\eta[\nabla u + (\nabla u)^T]) \quad (2)$$

The conservation of Energy with heat generation Q

$$\rho C_p \frac{\partial T}{\partial t} + \nabla \cdot (-K \nabla T) = Q - \rho C_p u \cdot \nabla T \quad (3)$$

$$\text{where } Q = -\Delta H_p K_p \lambda_0 M \quad (4)$$

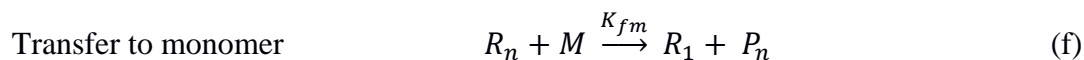
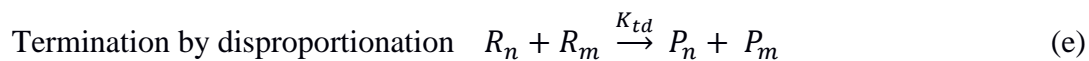
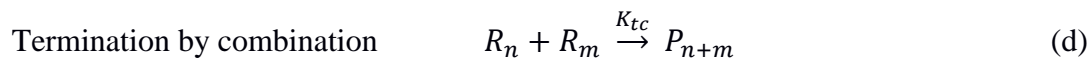
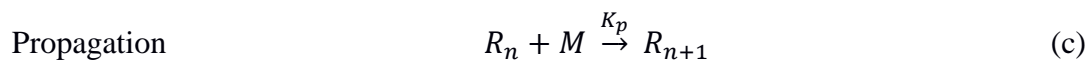
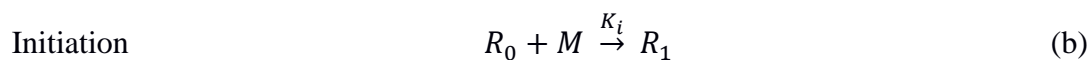
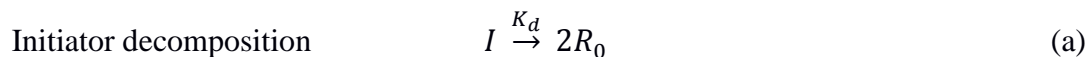
The conservation of Chemical species

$$\frac{\partial C_i}{\partial t} + \nabla \cdot (-D_i \nabla C_i + C_i u) = R_i \quad (5)$$

The chemical species were modeled as passive scalars and the generation term R_i (Equation 5) for each chemical species is presented in next section.

1.2. Kinetic Model of FRP

The various steps of kinetic model considered^[6] in this work are given in Scheme 1.



16
17 Scheme 1- Kinetic scheme for free radical polymerization as used in this work

18 19 **1.3. Mathematical Model of FRP**

20
21
22 The mathematical model^[16] studied in this work was based on the method of moments. λ_0 , λ_1
23 and λ_2 were zeroth, first and second order moments of the live polymer chain length
24 distributions whereas μ_0 , μ_1 and μ_2 were zeroth, first and second order of moments of dead
25 polymer chain length distribution. The model is presented in Appendix-A in Supplementary
26 Information.
27
28
29
30
31
32
33

34 35 **1.4. New Transformation**

36
37 The new transformation (NT) used in this work is given in Appendix-B in Supplementary
38 Information. For details, please refer to our previous work.^[7]
39
40
41

42 43 **1.5. Physical and Chemical Data**

44 Physical and chemical data used for MMA were taken from various references.^[5,17-24]
45
46

47 48 **2. Methodology**

49 50 **2.1. Numerical Modeling**

51 The residence time within all the flow microreactors were kept at about 12 hrs. A reputed and
52 proven commercial CFD software CFD-ACE+ was used.^[6,7] CFD-GEOM was used for
53 geometry and grid generation. It worked for both structured and unstructured grid as shown in
54 our previous work.^[6,7] Structured grid was used in this work for all geometries. Detailed mesh
55
56
57
58
59
60
61
62
63
64
65

1 independency test was carried out presented in a later section. CFD-ACE was used for CFD
2 simulations and the flow, heat and scalar modules available in it were used for the same. CFD-
3
4 VIEW was used for post-processing of all the simulations.
5

6
7 Five chemical species whose generation terms were represented by Equation (A1), (A2), (A9)
8
9 - (A11) were modeled as passive scalars, denoted as Scalar1-5 respectively. The spatial
10
11 distribution of velocity and all the five scalars were taken to be 3rd order so as to improve the
12
13 numerical accuracy and to reduce the numerical diffusion in the simulations. Conjugated
14
15 gradient squared (CGS) + Preconditioner solver was selected for velocity, enthalpy and all five
16
17 passive scalars whereas Algebraic Multigrid (AMG) solver was selected for pressure.
18
19 SIMPLEC algorithm was used for pressure-velocity coupling in the CFD code. Relaxation
20
21 parameters for various variables like velocity, pressure, passive scalars etc. were adjusted to
22
23 ensure convergence of the simulation. The simulations were assumed to be converged when the
24
25 residual error ratio reduced below 10^{-8} for all the variables. The relaxation parameters were also
26
27 adjusted to increase the rate of convergence and to reduce the simulation time. Flow-average
28
29 values of all the variables were evaluated at reactor outlet.
30
31
32
33
34

35
36 The reaction conditions and reactor operating conditions as given in **Table 1** were same as they
37
38 were taken in our previous work^[6] except for the feed condition at reactor inlet. In current study,
39
40 the feed was fully mixed in terms of initiator and monomer concentration with 30% dilution by
41
42 solvent at inlet. The feed condition for all the cases was considered same. At the inlet, velocity
43
44 profile was taken to be parabolic to model fully developed flow. The concentration profiles of
45
46 various chemical species were taken to be flat to model fully mixed feed condition. The inlet
47
48 temperature of the feed to the reactor was taken to be same as isothermal wall temperature of
49
50 the reactor i.e. 70°C. No-slip at reactor wall, zero flux for all the passive scalars across the wall
51
52 and isothermal condition at reactor wall were taken as boundary conditions. Due to NT, the
53
54
55
56
57
58
59
60
61
62
63
64
65

1 values of scalars were normalized. Hence the values of Scalar 1 and 2 were taken to be 1 and
 2 Scalar 3-5 were taken to be 0 at inlet, i.e. only initiator and monomer were present in the feed.
 3
 4 Two sets of simulations were conducted : one for coupled transport processes by modeling
 5 variation of FTTP and another was decoupled transport processes modeled through constant
 6 FTTP. This was done to evaluate the effect of coupling the transport processes over the results
 7 obtained through decoupled transport processes case. These simulations were carried out
 8 against the discrete variation of diffusion coefficient as it was done in our previous work.^[6,7]
 9
 10 The models for variation of density, viscosity and thermal conductivity were taken from
 11 Baillagou et al.^[5]

12 One simulation with continuous variation of diffusion coefficient with conversion for different
 13 chemical species with constant FTTP was also carried out for each microreactor geometry for
 14 same operating conditions.

15 The continuous variation in diffusion coefficients was modeled using free volume theory. The
 16 theory for calculating diffusion coefficient was developed by Vrentas and Duda^[14,15] for
 17 predicting diffusion coefficient. This was the most successful theory for predicting diffusion
 18 coefficient so far. Expressions to calculate these diffusion coefficients are given below, details
 19 of which could be found elsewhere.^[13]

$$20 \quad D_M = D_{M0} \exp \left[-\frac{\gamma_M \xi_{MP}}{V_f} \left(\frac{\omega_M V_M^*}{\xi_{MP}} + \omega_P V_P^* + \frac{\omega_S V_S^*}{\xi_{SP}} \right) \right] \quad (6)$$

$$21 \quad D_P = \frac{D_{P0}}{\left(\frac{MW_M^2}{MW_M} \right)} \cdot \exp \left[-\frac{\gamma_P}{V_f} \left(\frac{\omega_M V_M^*}{\xi_{MP}} + \omega_P V_P^* + \frac{\omega_S V_S^*}{\xi_{SP}} \right) + \frac{\gamma_P}{\xi_{MP} V_{fM}} \right] \quad (7)$$

22 where:

$$23 \quad D_{P0} = \frac{k_B T}{6\pi\eta_M(R_H)_0} \quad (8)$$

$$24 \quad (R_H)_0 = \left(\frac{3}{10\pi N_A} [\eta]_0 MW_M \right)^{\frac{1}{3}} \quad (9)$$

$$25 \quad [\eta]_0 = K_{MH} \cdot MW_M^{\alpha_{MH}} \quad (10)$$

$$V_f = \omega_M V_M^* V_{fM} + \omega_P V_P^* V_{fP} + \omega_S V_S^* V_{fS} \quad (11)$$

$$\xi_{kP} = \frac{M_{jk} V_k^*}{M_{jP} V_P^*} \quad (12)$$

The effect on various reaction parameters like X_M , PDI and DP_n with discrete variation in diffusion coefficient of chemical species was studied. During discrete variation of diffusion coefficient among simulations, the value of diffusion coefficient was assumed to be constant and same for all the passive scalars (chemical species) in a given simulation. For continuously varying diffusion coefficients case, first two passive scalars – 1 & 2, representing initiator (in solvent) and monomer, were considered to have same value of diffusion coefficients and thus calculated using Equation (6). The value of diffusion coefficients for the rest three passive scalars was considered same as these scalars represented dead polymer chains and were calculated using Equation (7).

2.2. Meshing

CFD-GEOM was used to generate the reactor geometry. A specific program was developed to generate CFIR of desired geometrical specification including pitch, number of turns in between the two bends, number of bends, curvature ratio and number of grid points in axial flow. Dimensions of all the three reactors were kept identical especially in terms of the length to have identical residence time and number of turns in integral value in both CTR and CFIR to the extent possible (**Table 2**). Structured grid was used for all the geometries. Square mesh was selected for circular cross-section. Only the upper half was modeled for STR due to axial symmetry but its cross-sectional mesh density was kept same as that of CTR and CFIR. The structured mesh and geometry of the three reactors were shown in **Figure 1**.

2.3. Simulation

In our previous work,^[16] an analytical solution (AS) of the set of differential equations constituting the mathematical model of FRP (as given in Appendix-A) was derived for ideal batch reactor conditions, i.e. isothermal, well mixed, batch reactor solution

1 homopolymerization before gel/glass/cage effect. To check the correctness of coding of
2 mathematical model along with NT, STR with coarse meshing was first simulated as batch
3 reactor with same operating conditions already mentioned except for no flow at inlet and outlet.
4
5 The values of Scalar 1 and 2 were taken to be 1 and the value for Scalar 3-5 was taken as 0 each
6
7 for the whole volume as the initial value for the simulation. The simulation was transient in
8
9 nature with the total time of simulation kept same as residence time. Its results were compared
10
11 with AS under same conditions.
12
13
14
15

16 The batch reactor results with time were theoretically applicable for the plug flow reactor with
17 distance along flow. So, STR was then simulated as plug flow reactor (PFR) with coarse
18 meshing by imposing flat velocity and flat concentration profile at inlet and same inlet velocity
19 at wall instead of no-slip as boundary condition. The other operating conditions were kept same
20 as already mentioned. The results were again compared with AS under similar conditions. For
21 both above tests, the data taken for monomer was for styrene. For details about its chemical
22 data, please refer to our previous work.^[6,7] Both these test simulations would validate the coding
23 of the mathematical model in CFD beyond doubt.
24
25
26
27
28
29
30
31
32
33
34
35

36 After this, extensive mesh independence tests were carried out for all the three reactor
37 geometries individually. Extensive mesh independence analysis was done for a given reactor
38 geometry for fully mixed feed condition. For each reactor geometry, three different diffusion
39 coefficients ($D = 1 \times 10^{-12}, 1 \times 10^{-10}, 1 \times 10^{-8} \text{ m}^2/\text{s}$) were used to cover the complete
40 range of variation of diffusion coefficient under study. Mesh density was changed in both
41 radical and axial directions and then it was checked for convergence. Finally, only four most
42 suitable cases of grids were selected for further evaluation where all the variables satisfactorily
43 became mesh independent. These four cases arose from the combination of changes in axial
44 direction mesh density and cross-sectional mesh density. All the variables were to be made
45 independent of mesh for that particular mesh to be selected.
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

Once the final mesh was selected, all the proposed CFD simulations were then carried out. Same final mesh was used for continuously varying diffusion coefficient case.

3. Results and Discussion

The result of STR modeled as batch reactor is shown in **Figure 2**. The result shows the values of five Scalars plotted on the same axis. Due to NT used, their values are normalized and dimensionless in terms of concentration. It matched exactly with AS. This proves that the code related to implementation of rate equations for scalar 1-5 as source terms in their respective equations, is correctly implemented.

The results for STR as PFR compared to AS are given in **Table 3**. As can be seen, the results matched excellently with AS obtained under the same reactor conditions. This proved that code related to the scalar1-5 equations was properly integrated with flow and energy equations

Thus, both batch type reactor as well as plug flow type reactor simulations validated the correctness of the implementation of the code related to reaction equations of scalar 1-5 within the software for simulation along with the correct implementation of the NT.

Extensive mesh independence analysis was done for all variables. One such variable, monomer conversion X_M , is shown in **Table 4** for the STR only. The same procedure was also used for CTR and CFIR also.

After mesh independence test, a common mesh was found to be suitable for the whole range of variation of values of diffusion coefficient taken under study for a given reactor geometry. In this problem, the values of variables were found to be more dependent upon mesh density in flow direction rather than on cross-sectional mesh density as highlighted by **Table 4**. The same observation was made for all the three reactor geometries. This helped in selecting coarse mesh density for cross-section to reduce the total number of mesh point without affecting the results.

The final mesh selected for a given geometry for mix inlet condition is given in **Table 5**.

1 The values of relaxation parameters were found to have huge impact on the rate as well as the
2 level of convergence during our study. But once a given simulation was found to converge
3
4 (based on residual error ratio value criteria already mentioned), the values of variables in the
5
6 converged solution were found to be independent of relaxation parameter values. The values of
7
8 relaxation parameters were found to be affected by the values of diffusivity coefficient. The
9
10 values chosen for relaxation parameters were found to reduce the residual error ratio value to
11
12 levels below 10^{-8} and thus improving the accuracy of the simulations. Furthermore, they also
13
14 increased the rate of convergence. The stopping criteria of residual error ratio value was
15
16 achieved in 150-3000 iterations depending on the simulation.
17
18
19
20

21 For constant FTPP case, the convergence was obtained over a large range of diffusion
22
23 coefficient values ranging from $1 \times 10^{-12} \text{ m}^2/\text{sto}$ to $1 \times 10^{-8} \text{ m}^2/\text{s}$ for all the three reactor
24
25 geometries under study. For variable FTPP case, the convergence could be obtained for limited
26
27 values of diffusion coefficient: in five cases for STR and in just three cases each for CTR and
28
29 CFIR. Simulations for varying diffusion coefficient could only be converged for the case of
30
31 constant FTPP case.
32
33
34
35

36 **Figure 3** shows some important results about monomer conversion, X_M . For all the three reactor
37
38 geometries, X_M was found to be independent of the geometry for both the cases of constant
39
40 (decoupled transport processes case) and variable FTPP (coupled transport processes case).
41
42 Although the trend as well as values of X_M differed from each other for these two cases. The
43
44 geometry independence of X_M could probably be due to mixed feed condition which lowered
45
46 the requirement for mixing within the microreactor compared to unmixed condition as shown
47
48 in our previous work^[6,7] and other published results.^[3,4] The values of X_M predicted for the
49
50 coupled transport processes case were lower compared to the one predicted for decoupled
51
52 transport processes case. Besides this, for decoupled case, the variation in X_M value was small
53
54 over the complete range of variation of diffusion coefficient. Contrary to this, for coupled case,
55
56
57
58
59
60
61
62
63
64
65

1 there was appreciable decrease in X_M when the value of diffusion coefficient was decreased.
2 This seemed to be more realistic as decrease in value of diffusion coefficient would decrease
3 radial mixing. In absence of proper radial mixing, X_M in the central portion of the flow would
4 remain low because it would experience less residence time due to higher velocity in and around
5 the center of the tube. This clearly establishes the importance of modeling the variation in FTPP
6 over constant ones. This meant that the modeling of transport processes as coupled one is
7 necessary to obtain physically correct results for FRP in tubular microreactors.
8
9

10 **Figure 4** shows the results for number average chain length, DP_n . It also exhibited geometry
11 independence similar to X_M in **Figure 3** for both the cases of variable and constant FTPP. With
12 respect to trend, DP_n increased as the value of diffusion coefficient decreased for both the
13 cases. In FRP, DP_n decreases as X_M increases. Decreased diffusion coefficient lowered X_M as
14 seen in **Figure 3**. So, lower X_M due to lower diffusion coefficient made DP_n to rise. Here
15 again, similar to X_M , DP_n values were also predicted to be lower in case of coupled transport
16 processes case compared to decoupled transport processes case.
17
18

19 **Figure 5** shows the results related to polydispersity index, PDI . Here again, the values of PDI
20 were found to be independent of reactor geometry for both the cases of constant and variable
21 FTPP. The predictions of coupled transport processes case were significantly lower than that
22 for the decoupled transport processes case. PDI is one of the most important parameters
23 determining the quality of the polymer product, so its realistic prediction is of great practical
24 importance and hence, is highly desirable. The predicted values of DP_n did not differ much
25 from each other for decoupled and coupled transport processes cases. Whereas, the predicted
26 values of PDI differed from each other by about 70% for the two cases, where predicted values
27 for coupled transport processes case were being at lower side.
28
29

30 **Figure 6** shows the variation of density at reactor outlet with diffusion coefficient for variable
31 FTPP case. The increase in density with increase in diffusion coefficient was understandable
32
33

1 from the point of view of corresponding X_M as shown in **Figure 3**. The increase in density along
2 the flow with monomer conversion is important from the fact that increased density would lead
3 to decreased velocity to conserve the mass flow. This would affect both the residence time and
4 residence time distribution inside the reactor as per the reactor geometry. This would not be the
5 case for residence time in case of constant density model.
6
7
8
9

10 **Figure 7** shows the results for viscosity variation at reactor outlet. This is one of the properties
11 in the polymerization reactions which changes by about 4 – 6 orders for full conversion
12 depending on the monomer-polymer system. Besides this, significant changes in viscosity could
13 affect the flow profile as well as mixing and thus heat transfer. Viscosity was found to be
14 increased by 6 orders in our simulations. The viscosity at outlet increased with an increase in
15 diffusion coefficient. This was because of the increased conversion that led to more polymer
16 fraction in the system, which in turn increased the viscosity. As a consequence, the pressure
17 drop across the reactor also increased. Variation of viscosity, pressure drop and density are
18 shown in **Figures 8-10** respectively for each reactor geometry. Great variation in density and
19 viscosity clearly proved the importance of modeling their variation and thus proved the
20 necessity of coupling the transport processes with reaction and mixing.
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38

39 The results for the single case of CFD simulation for all the three reactor geometries with
40 continuously varying diffusion coefficient for various chemical species and constant FTPP are
41 summarized in **Table 6**.
42
43
44
45

46 Here we could observe that the results for X_M and PDI were closer to the one predicted by
47 variable FTPP case with discrete variation of diffusion coefficient. On the other hand, DPn was
48 predicted higher and was closer to constant FTPP case. Again the results were found to be
49 independent of the geometry for all the three reactor geometries.
50
51
52
53
54
55

56 Despite huge variation in viscosity and moderate changes in density, no significant variation of
57 thermal conductivity was observed. The temperature variation across the cross section differed
58
59
60
61
62
63
64
65

1 only by 0.1 K even for variable FTTP case simulations. Thus, truly isothermal condition was
2 observed even during high viscosity variation and density changes. So, modeling thermal
3 conductivity as constant would be a good assumption without affecting any results. However,
4 properties like density and viscosity had significant impact on the results of the simulations as
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

Conclusions

Three microreactor geometries with gradual change in geometry were taken for study through simulation of FRP under mixed feed condition at reactor inlet. The effects of variation of FTTP case compared to constant FTTP case with discrete variation of diffusion coefficient were studied. This was done to observe the importance of modelling the coupling of transport process with chemical reaction in microreactors. One case of varying diffusion coefficient with constant FTTP was also studied. The significant differences were observed in the predictions of X_M , DP_n and PDI between the variable and constant FTTP cases for the given condition of mixed feed at reactor inlet. The results were found to be closer to physical reality for the variable FTTP case. This clearly established the importance of modeling coupled transport processes with chemical reaction in tubular microreactors. Contrary to expectation, the results obtained were found to be independent of reactor geometries under consideration for either cases. In Appendix-D, the CFIR was shown to exhibit chaotic advection even at such a low inlet Reynolds number of 0.06 thus exhibiting improved mixing. CFIR seemed to be a promising microreactor for polymerization as shown by Parida et al.^[25,26] for atom transfer radical polymerization but current study did not get any such results despite having similar (though not same) reaction system. Both the models - the variable FTTP model alongwith discrete variation of diffusion coefficient and Constant FTTP model with continuously varying diffusion coefficient, were definitely an improvement over constant FTTP model with discrete variation of diffusion coefficient. But both could not predict the improved results for CFIR despite having

1 improved mixing. Clearly, to evaluate CFIR more thoroughly, a more comprehensive modeling
2 is required. This might include complete variation of FTTP along with continuous variation of
3
4 diffusion coefficient which would be part of future work.
5
6

7 **Supporting Information**

8
9 Supporting Information is available from the Wiley Online Library
10

11
12 **Appendix-A:** Mathematical model for free radical polymerization as used in this work.
13

14
15 **Appendix-B:** Zhu Transformation and New transformation.
16

17
18 **Appendix-C:** Expression for the variations in viscosity, density and thermal conductivity for
19
20 MMA.
21

22
23 **Appendix-D:** Visualizing mixing inside the three tubular microreactors using mass-less
24
25 tracer particles
26
27
28
29
30

31 **Appendix/Nomenclature/Abbreviations**

| | | |
|----|----------|---|
| 32 | | |
| 33 | | |
| 34 | A_H | Area for heat transfer, m^2 |
| 35 | | |
| 36 | C_M | $\frac{K_{fm}}{K_p}$, dimensionless |
| 37 | | |
| 38 | | |
| 39 | | |
| 40 | C_p | Specific heat capacity of mixture, cal/g/°C |
| 41 | | |
| 42 | C_T | $\frac{K_{td}}{K_{tc}}$, dimensionless |
| 43 | | |
| 44 | | |
| 45 | DP_n | Number averaged degree of polymerization |
| 46 | | |
| 47 | | |
| 48 | I | Initiator concentration, mol/l |
| 49 | | |
| 50 | | |
| 51 | K_d | Dissociation rate coefficient, min^{-1} |
| 52 | | |
| 53 | K_{fm} | Transfer to monomer rate coefficient, l/(mol.min) |
| 54 | | |
| 55 | | |
| 56 | K_i | Kinetic rate constant for initiation, s^{-1} |
| 57 | | |
| 58 | K_p | Propagation rate coefficient, l/(mol.min) |
| 59 | | |
| 60 | | |
| 61 | | |
| 62 | | |
| 63 | | |
| 64 | | |
| 65 | | |

| | | |
|----|-------------|--|
| 1 | K_{pr} | $K_p + K_{fm} = (1 + C_M)K_p$, l/(mol.min) |
| 2 | K_t | $K_{tc} + K_{td}$, l/(mol.min) |
| 3 | | |
| 4 | K_{tc} | Termination by combination rate coefficient, l/(mol.min) |
| 5 | | |
| 6 | | |
| 7 | K_{td} | Termination by disproportionation rate coefficient, l/(mol.min) |
| 8 | | |
| 9 | | |
| 10 | L | Kinetic chain length, $\frac{K_{pr}M\lambda_0}{2fK_dI}$ |
| 11 | | |
| 12 | \acute{L} | $L \cdot \left(\frac{1-R_{MM}}{1+R_pL}\right) = L \cdot \left(\frac{1-R_M}{1+R_pL}\right)$ |
| 13 | | |
| 14 | | |
| 15 | | |
| 16 | M | Monomer concentration, mol/l |
| 17 | | |
| 18 | | |
| 19 | MW | Molecular weight, g/mol |
| 20 | | |
| 21 | MW_n | Number averaged chain length of polymer, g/mol |
| 22 | | |
| 23 | | |
| 24 | MW_w | Weight averaged chain length of polymer, g/mol |
| 25 | | |
| 26 | PDI | Polydispersity index, dimensionless |
| 27 | | |
| 28 | | |
| 29 | P_n | Dead polymer chain length of n no. of monomer units |
| 30 | | |
| 31 | | |
| 32 | R | Universal gas constant, 1.986 cal/mol/K |
| 33 | | |
| 34 | R_0 | Zero order radical obtained from initiator dissociation |
| 35 | | |
| 36 | R_M | $\frac{K_{fm}}{K_p+K_{fm}} = \frac{K_{fm}}{K_{pr}} = \frac{C_M}{1+C_M}$ |
| 37 | | |
| 38 | | |
| 39 | | |
| 40 | R_{MM} | R_M |
| 41 | | |
| 42 | R_n | Live polymer chain length of n no. of monomer units |
| 43 | | |
| 44 | | |
| 45 | R_T | $\frac{K_{tc}}{K_{tc}+K_{td}} = \frac{K_{tc}}{K_t} = \frac{1}{1+C_T}$, dimensionless |
| 46 | | |
| 47 | | |
| 48 | T | Temperature, K |
| 49 | | |
| 50 | | |
| 51 | T_{bath} | Temperature of heat sink, K |
| 52 | | |
| 53 | U | Overall heat transfer coefficient, W/m ² /K |
| 54 | | |
| 55 | V_R | Volume of solution at any time t, liter |
| 56 | | |
| 57 | | |
| 58 | V_{R0} | Initial volume of solution at t0, liter |
| 59 | | |
| 60 | | |
| 61 | | |
| 62 | | |
| 63 | | |
| 64 | | |
| 65 | | |

| | | |
|----|-----------------|--|
| 1 | X_M | Monomer conversion, dimensionless |
| 2 | f | Initiator efficiency, dimensionless |
| 3 | | |
| 4 | f_s | Initial Solvent volume fraction, dimensionless |
| 5 | | |
| 6 | | |
| 7 | f_v | Fractional free volume, dimensionless |
| 8 | | |
| 9 | | |
| 10 | t | Time , min |
| 11 | | |
| 12 | u | Velocity, m/s |
| 13 | | |
| 14 | ΔH_p | Heat of reaction, cal/mol |
| 15 | | |
| 16 | | |
| 17 | β | Ratio of solvent volume to non-solvent volume, dimensionless |
| 18 | | |
| 19 | ε | Volume contraction factor corrected for solvent volume fraction, dimensionless |
| 20 | | |
| 21 | | |
| 22 | ε_0 | Volume contraction factor without solvent volume fraction, dimensionless |
| 23 | | |
| 24 | λ_0 | Zeroth order moment for live polymer chain length distribution, mol/l |
| 25 | | |
| 26 | | |
| 27 | λ_1 | First order moment for live polymer chain length distribution, mol/l |
| 28 | | |
| 29 | | |
| 30 | λ_2 | Second order moment for live polymer chain length distribution, mol/l |
| 31 | | |
| 32 | μ_0 | Zeroth order moment for dead polymer chain length distribution, mol/l |
| 33 | | |
| 34 | | |
| 35 | μ_1 | First order moment for dead polymer chain length distribution, mol/l |
| 36 | | |
| 37 | μ_2 | Second order moment for dead polymer chain length distribution, mol/l |
| 38 | | |
| 39 | | |
| 40 | ρ | Mixture density, g/cm ³ |
| 41 | | |
| 42 | Φ | Volume fraction, dimensionless |
| 43 | | |
| 44 | | |
| 45 | η | Dynamic viscosity, cP |
| 46 | | |
| 47 | Subscript | |
| 48 | | |
| 49 | M | <i>Monomer</i> |
| 50 | | |
| 51 | | |
| 52 | P | <i>Polymer</i> |
| 53 | | |
| 54 | S | <i>Solvent</i> |
| 55 | | |
| 56 | | |
| 57 | I | <i>Initiator</i> |
| 58 | | |
| 59 | | |
| 60 | | |
| 61 | | |
| 62 | | |
| 63 | | |
| 64 | | |
| 65 | | |

0 *At time t=0*

1
2
3
4
5 Acknowledgements: The financial support by ANR grant No. 09-CP2D-DIP² is greatly
6
7 appreciated.
8
9

10
11
12 Keywords: coupled problem, CFD, mixing, free radical polymerization, coiled flow inverter
13
14 microreactor
15
16
17
18

- 19 [1] J. Y. Kim, R. L. Laurence, *Korean J Chem Eng*, **1998**, 15 (3), 273.
20
21 [2] V. Hessel, H. Lowe, F. Schonfeld, *Chem Eng Sci*, **2005**, 60 (8-9), 2479.
22
23 [3] M. M. Mandal, C. Serra, Y. Hoarau, K. D. P. Nigam, *Microfluid Nanofluid*, **2011**, 10
24
25 (2), 415.
26
27 [4] a) C. Serra, G. Schlatter, N. Sary, F. Schonfeld, G. Hadziioannou, *Microfluid Nanofluid*,
28
29 **2007**, 3 (4), 451; b) C. Serra, N. Sary, G. Schlatter, G. Hadziioannou, V. Hessel, *Lab*
30
31 *Chip*, **2005**, 5, 966.
32
33 [5] P. E. Baillagou, D. S. Soong, *Polym Eng Sci*, **1985**, 25 (4), 212.
34
35 [6] D. K. Garg, C. A. Serra, Y. Hoarau, D. Parida, M. Bouquey, R. Muller, *Macromol Theor*
36
37 *Simul*, **2020**, <https://doi.org/10.1002/mats.202000008>.
38
39 [7] D. K. Garg, C. A. Serra, Y. Hoarau, D. Parida, M. Bouquey, R. Muller, *Microfluid*
40
41 *Nanofluid*, **2015**, 18, 1287.
42
43 [8] A. K. Saxena, K. D. P. Nigam, *Aiche J*, **1984**, 30 (3), 363.
44
45 [9] V. Kumar, M. Aggarwal, K. D. P. Nigam, *Chem Eng Sci*, **2006**, 61 (17), 5742.
46
47 [10] S. A. Berger, L. Talbot, L. S. Yao, *Annu Rev Fluid Mech*, **1983**, 15, 461.
48
49 [11] W. R. Dean, J. M. Hurst, *Philosophical Magazine Series 7*, **1927**, 4 (20), 77.
50
51 [12] C. M. White, *Proc. R. Soc. Lond. A*, **1929**, 123, 645.
52
53
54
55
56
57
58
59
60
61
62
63
64
65

- 1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65
- [13] N. Ramesh, P. K. Davis, J. M. Zielinski, R. P. Danner, J. L. Duda, *J Polym Sci Pol Phys*, **2011**, 49 (23), 1629.
- [14] J. S. Vrentas, J. L. Duda, *J Polym Sci Pol Phys*, **1977**, 15 (3), 417.
- [15] J. S. Vrentas, J. L. Duda, *J Polym Sci Pol Phys*, **1977**, 15 (3), 403.
- [16] D. K. Garg, C. A. Serra, Y. Hoarau, D. Parida, M. Bouquey, R. Muller, *Macromolecules*, **2014**, 47 (14), 4567.
- [17] A. Keramopoulos, C. Kiparissides, *J Appl Polym Sci*, **2003**, 88 (1), 161.
- [18] J. M. Zielinski, J. L. Duda, *Aiche J*, **1992**, 38 (3), 405.
- [19] P. E. Baillagou, D. S. Soong, *Chem Eng Sci*, **1985**, 40 (1), 75.
- [20] S. K. Soh, D. C. Sundberg, *J Polym Sci Pol Chem*, **1982**, 20, 1331.
- [21] S. K. Soh, D. C. Sundberg, *J Polym Sci Pol Chem*, **1982**, 20, 1345.
- [22] D. S. Achilias, C. Kiparissides, *J Macromol Sci R M C*, **1992**, C32 (2), 183.
- [23] J. Brandrup, in *Polymer Handbook*, (Eds: J. Brandrup, E. H. Immergut), Interscience Publishers, New York **1966**.
- [24] R. H. Shoulberg, J. A. Shetter, *J Appl Polym Sci*, **1962**, 6 (23), S32.
- [25] D. Parida, C.A. Serra, D.K. Garg, Y. Hoarau, R. Muller, M. Bouquey, *Macromolecular Reaction Engineering*, **2014**, 8 (8),597.
- [26] D. Parida, C.A. Serra, F. Bally, D.K. Garg, Y. Hoarau, F. Bally, R. Muller, M. Bouquey, *Macromolecules*, **2014**, 47 (10), 3282.

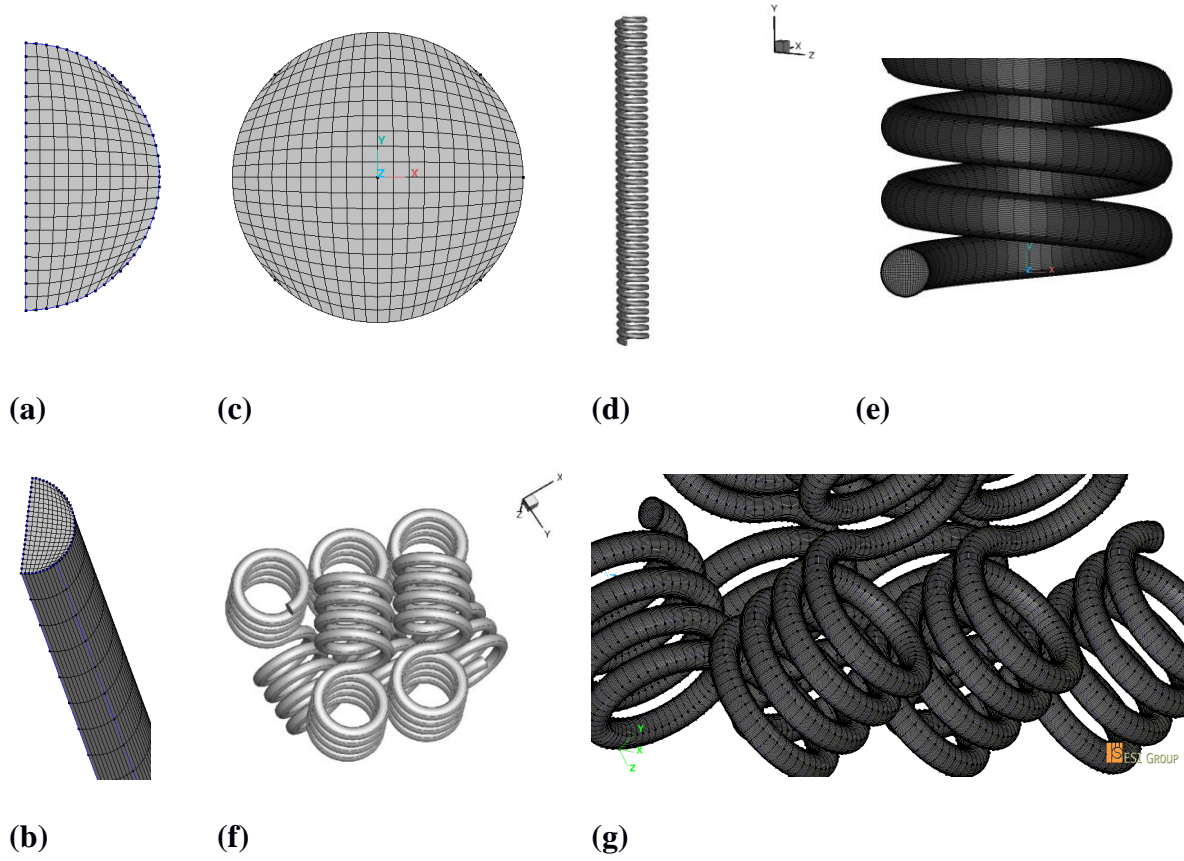


Figure 1. a) Cross section meshing of STR inlet, b) STR volume grid, c) cross section meshing of CTR and CFIR inlet, d) CTR general view, e) CTR volume grid, f) CFIR general view, g) CFIR volume grid.

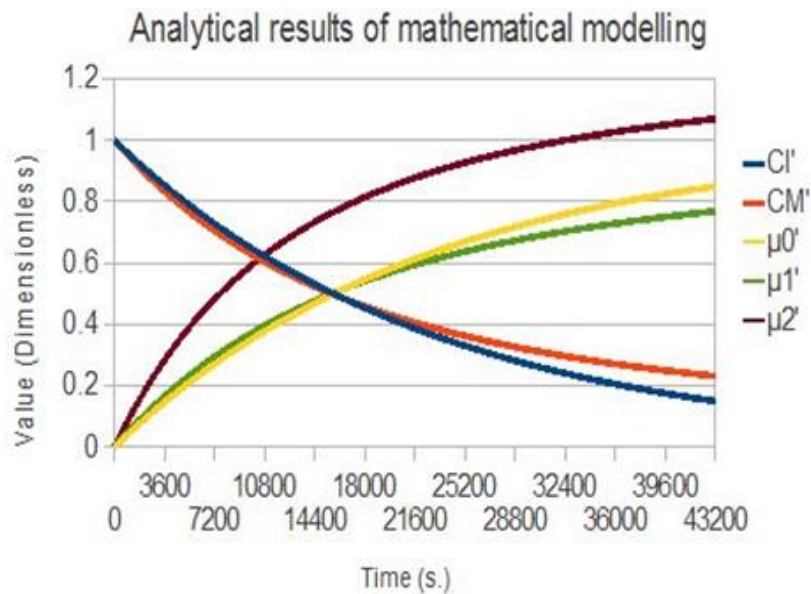


Figure 2. Comparison of results for STR modelled as well mixed isothermal batch reactor with the analytical solution under similar conditions.

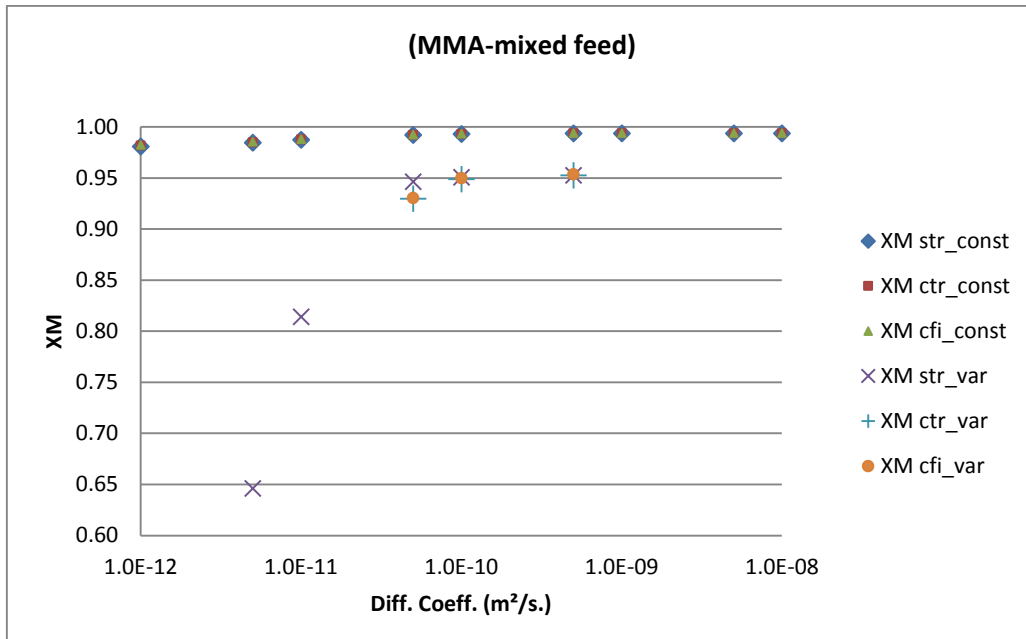


Figure 3. Monomer conversion (X_M) results for STR, CTR and CFIR for constant and variable FTTP.

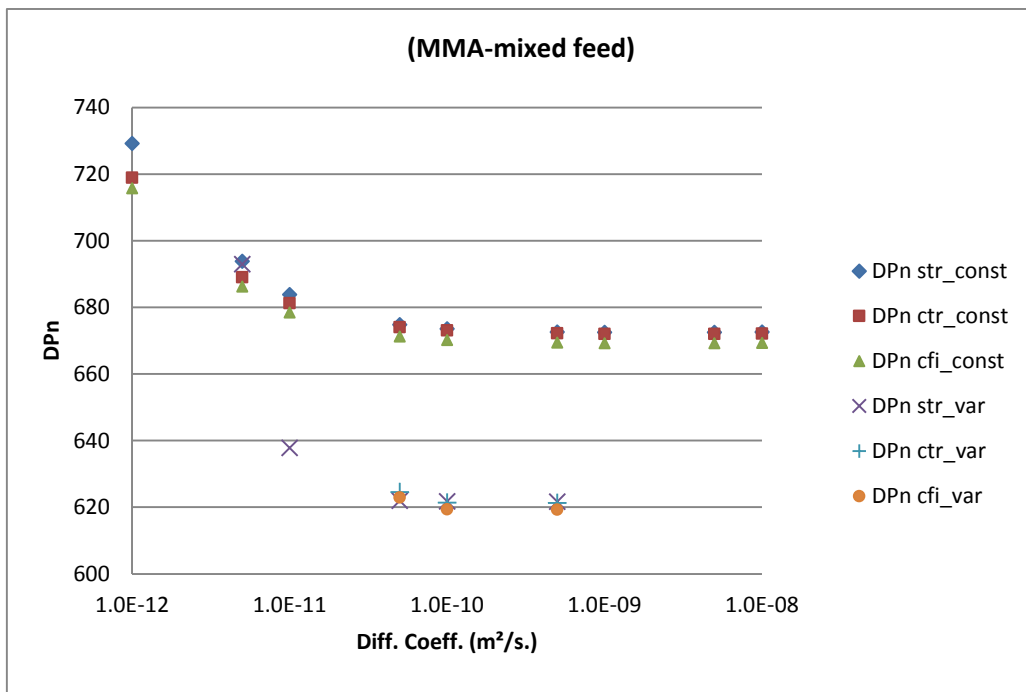


Figure 4. DP_n results for STR, CTR and CFIR for constant and variable FTTP cases.

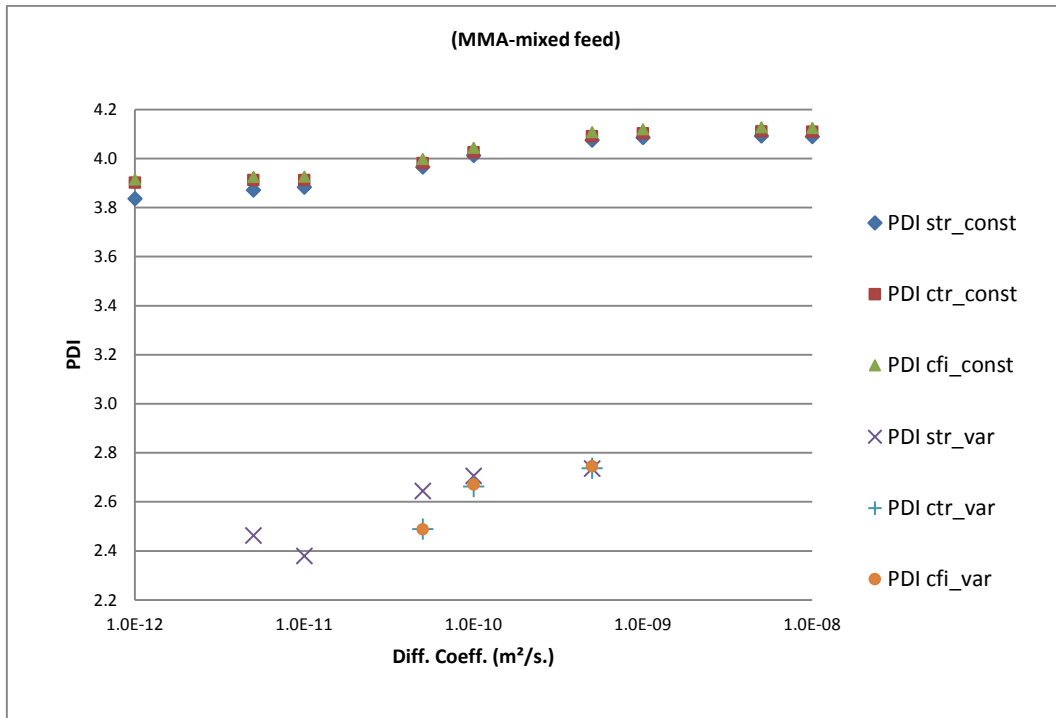


Figure 5. PDI results for STR, CTR and CFIR for constant and variable FTPP

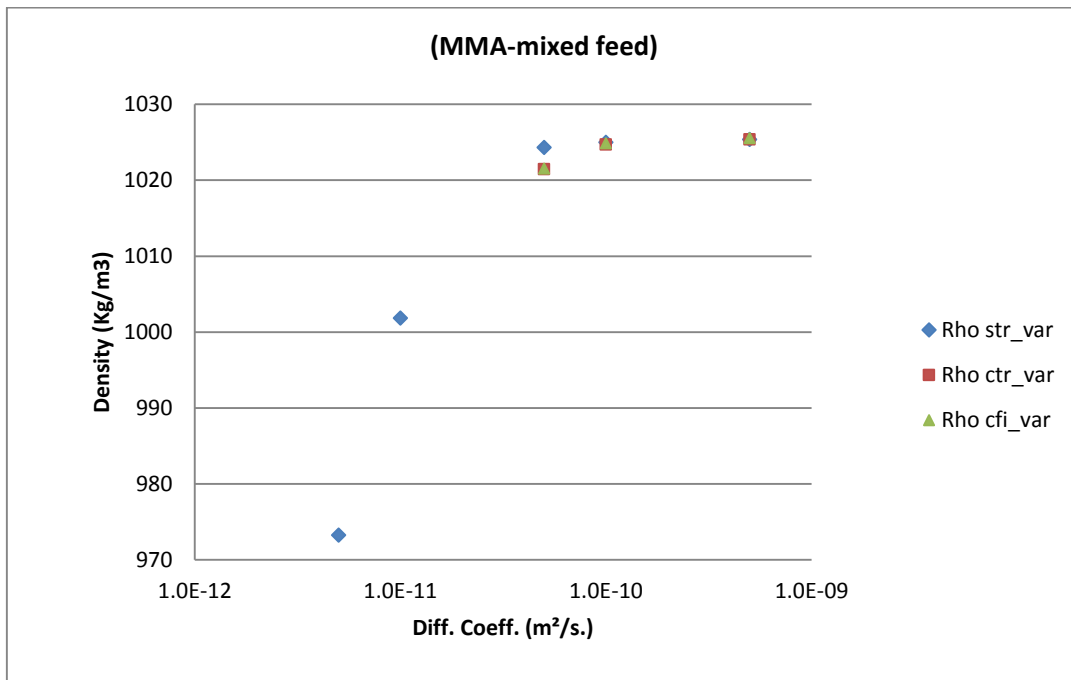


Figure 6. Density results for STR, CTR and CFIR for variable FTPP

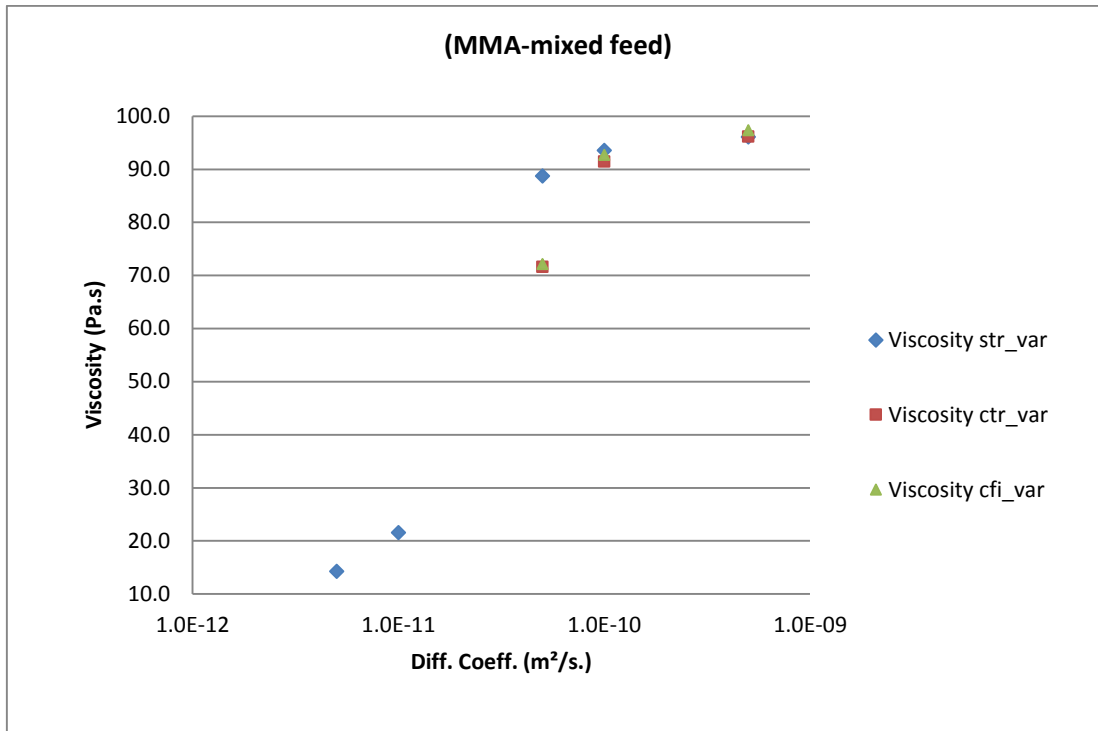


Figure 7. Viscosity results for STR, CTR and CFIR for variable FTPP

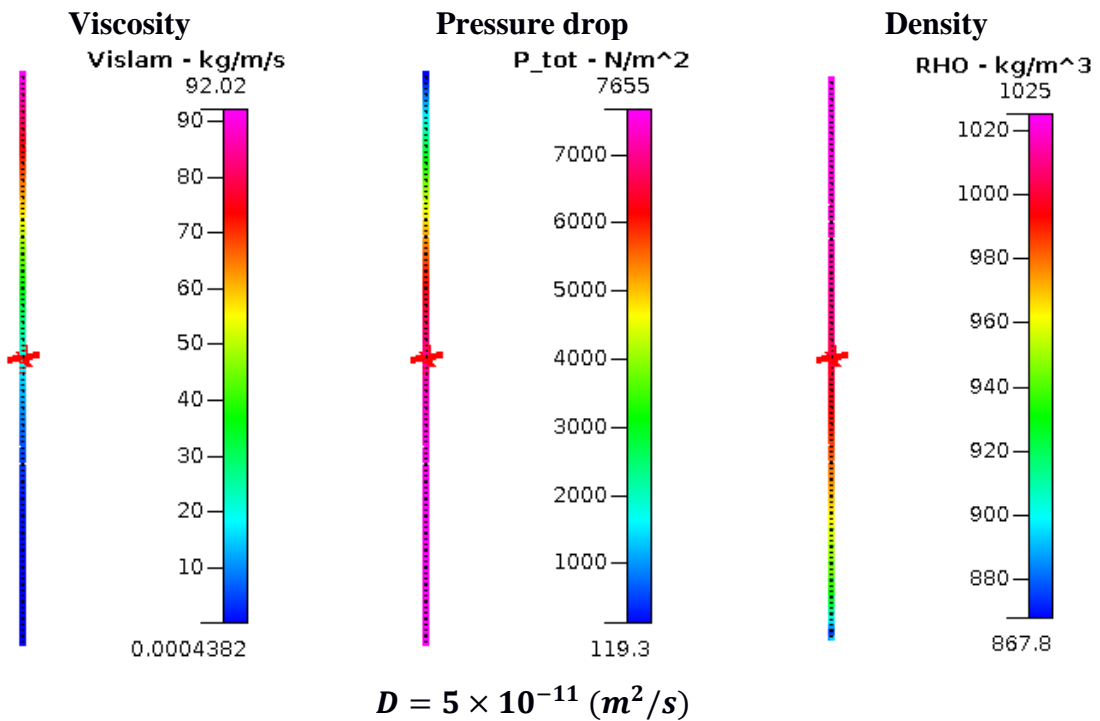
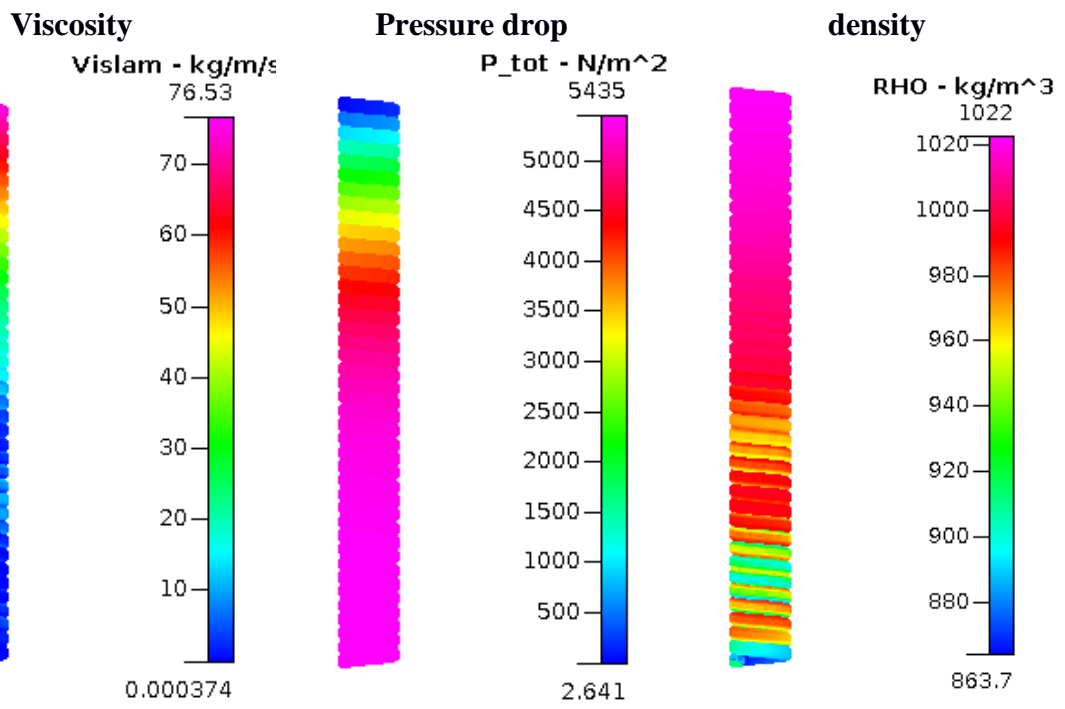
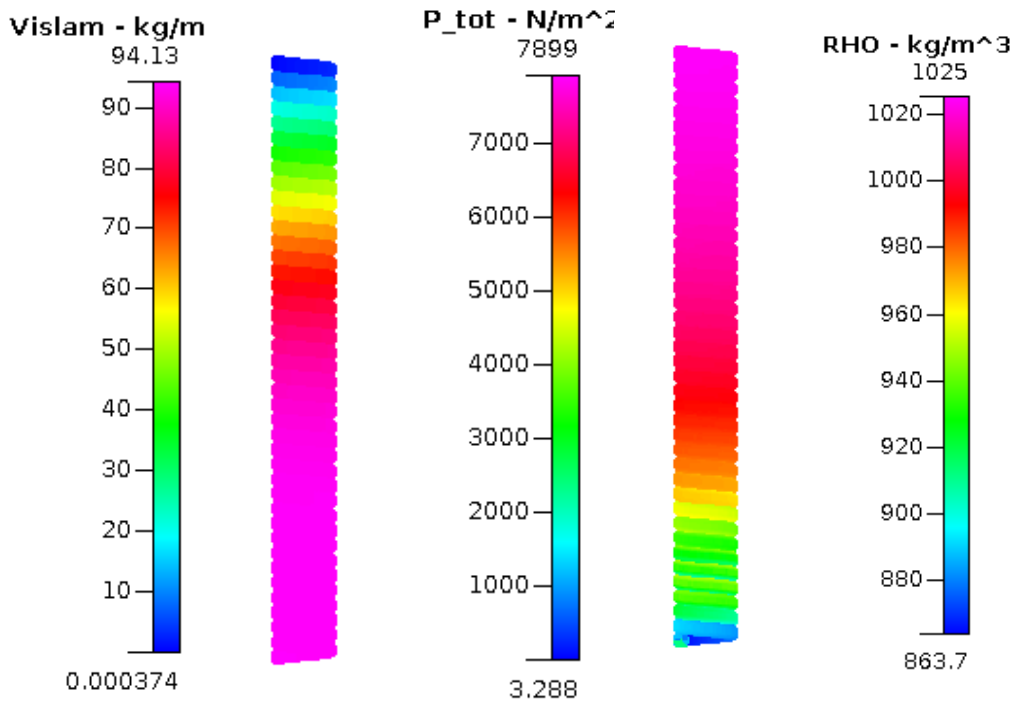


Figure 8. Viscosity, pressure drop and density variation throughout the volume of STR



$D = 5 \times 10^{-11} (m^2/s)$



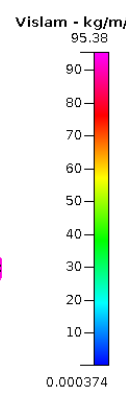
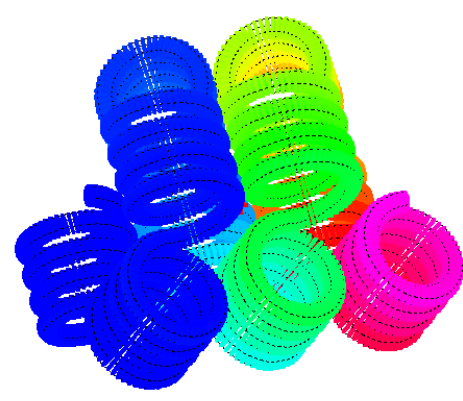
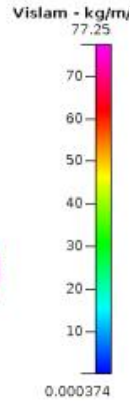
$D = 1 \times 10^{-10} (m^2/s)$

Figure 9. Viscosity, pressure drop and density variation throughout the volume of CTR

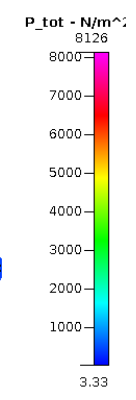
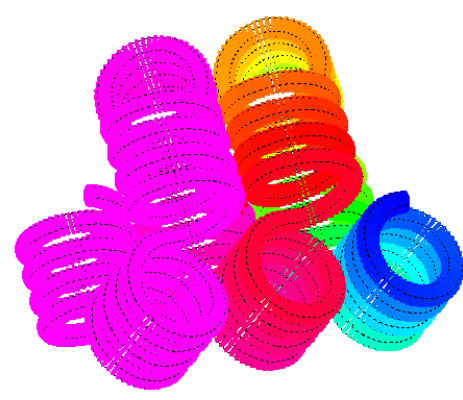
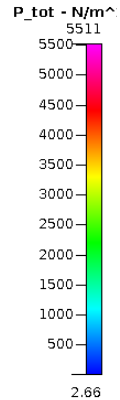
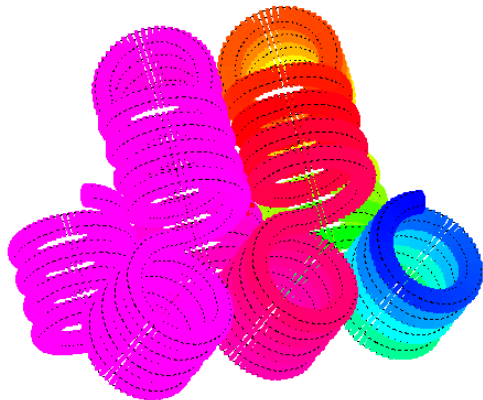
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

$D = 5 \times 10^{-11} \text{ (m}^2/\text{s)}$

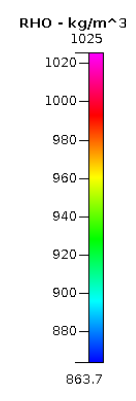
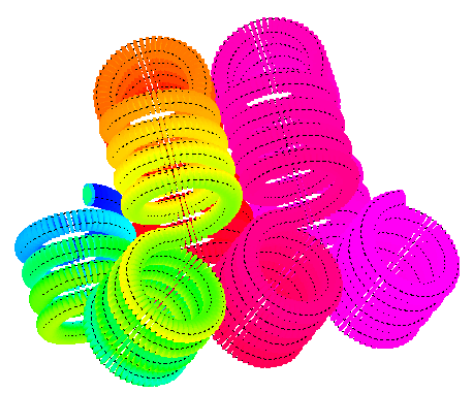
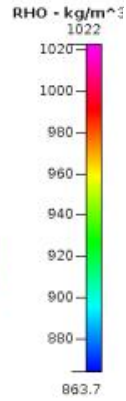
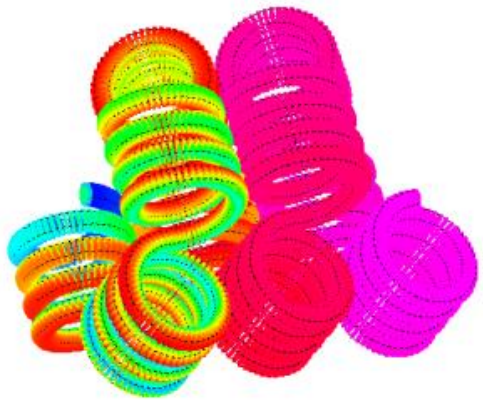
$D = 1 \times 10^{-10} \text{ (m}^2/\text{s)}$



Viscosity



Pressure drop



Density

Figure 10. Viscosity, pressure drop and density variation throughout the volume of CFIR

Table 1. Operating conditions and physical data for constant fluid physical properties simulations⁵

| Parameter | Value |
|---|--|
| Wall temperature (K) - constant | 343.15 |
| Inlet feed temperature (K) | 343.15 |
| Chemical species diffusion coefficient. (m ² /s) | from 1×10^{-12} to 1×10^{-8} |
| Fluid density(kg/m ³) | 1×10^3 |
| Fluid viscosity (Pa.s) | 1×10^{-3} |
| Fluid thermal conductivity (W/m/K) | 0.6 |
| Fluid specific heat (J/kg/K) | 4182 |
| Fluid velocity (m/s) | 2.9×10^{-5} |
| Inlet Reynolds number | 0.06 |
| Residence time (hrs) | 12 |

Table 2. Reactor data

| Reactor Type | Length (m) | Curvature ratio ^{a)} | No. of turns | Pitch (m) | Number of bends | Residence Time (s) | Excess length (%) |
|--------------|------------|-------------------------------|--------------|-----------|-----------------|--------------------|-------------------|
| STR | 1.252 | - | - | - | 0 | 43200 | 0 |
| CTR | 1.262 | 5 | 40 | 0.003 | 0 | 43546 | +0.8 |
| CFIR | 1.285 | 5 | 40 | 0.003 | 9 | 44340 | +2.6 |

^{a)} curvature ratio is the ratio between radius of coil and inner radius of tube.

Table 3. Comparison of the data from analytical solution and the simulation of STR as plug flow reactor.

| | Analytical solution | Plug flow simulation |
|-------------------|---------------------|----------------------|
| Conversion, X_M | 0.770093 | 0.770024 |
| PDI | 1.53879 | 1.53873 |
| DPn | 372.981 | 372.968 |

Table 4. Mesh independency result for X_M for fully mixed inlet to STR.

| Conversion, X_M | Axial, Z=10 | Z=50 | Z=100 | Z=200 | Z=500 |
|---------------------------------|-------------|--------|--------|--------|--------|
| 20x20 (cross-section) | 0.7621 | 0.7681 | 0.7682 | 0.7683 | 0.7683 |
| 30x30 | 0.7621 | 0.7681 | 0.7682 | 0.7683 | 0.7683 |
| 50x50 | 0.7621 | 0.7681 | 0.7683 | 0.7683 | 0.7683 |
| 100x100 | 0.7621 | 0.7681 | 0.7683 | 0.7683 | 0.7683 |

Table 5. Result of mesh independency analysis.

| Reactor Geometry | Mixed Feed Inlet | |
|------------------|------------------|----------------|
| | Cross section | Flow direction |
| STR | 20x20 | 100 |
| CTR | 20x20 | 55* |
| CFIR | 20x20 | 55* |

* For CTR and CFIR, this is the number of points in flow direction in one complete turn. So total number of points = 55 x (number of turns)

Table 6. Results for variable diffusion coefficient with constant thermo-physical properties

| | STR | CTR | CFIR |
|-------|------------|------------|-------------|
| X_M | 0.905 | 0.909 | 0.910 |
| PDI | 2.59 | 2.62 | 2.62 |
| DPn | 693 | 685 | 683 |

Author Photograph(s) ((40 mm wide × 50 mm high, grayscale))



Dr. Dhiraj Kumar Garg

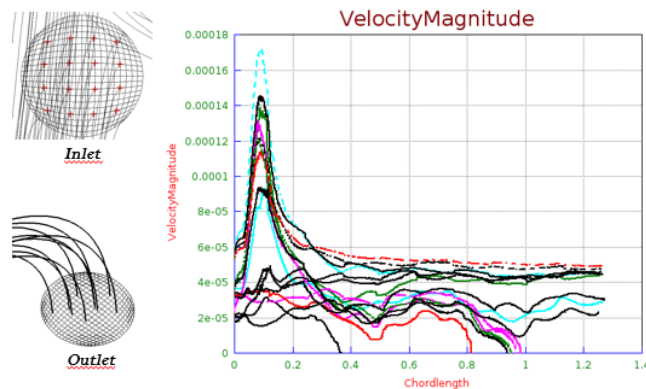
The importance of modeling polymerization with coupled transport processes in microreactor is clearly established in this work. It affects the prediction as well as the trend of various polymer characteristic parameters. Sensitive phenomena like chaotic advection in chaotic microreactor can be observed in a better way while modeling polymerization in it.

Dhiraj K. Garg, Christophe A. Serra, Yannick Hoarau, Dambarudhar Parida, Michel Bouquey, Rene Muller*

Numerical investigations of perfectly mixed condition at the inlet of free radical polymerization tubular microreactors of different geometries

ToC figure

CFD Analysis- CFIR, ($D = 5 \times 10^{-11}(\text{m}^2/\text{s})$, Variable)
Streamlines and velocity pattern for massless tracer particles



Supporting Information

APPENDICES

Numerical investigations of perfectly mixed condition at the inlet of free radical polymerization tubular microreactors of different geometries

Dhiraj K. Garg*, Christophe A. Serra, Yannick Hoarau, Dambarudhar Parida, Michel

Bouquey, Rene Muller

Appendix-A: Mathematical model for free radical polymerization as used in this work.

Initiator decomposition

$$\frac{-1}{V_R} \frac{d(I.V_R)}{dt} = K_d I \quad (\text{A1})$$

Monomer

$$\frac{-1}{V_R} \frac{d(M.V_R)}{dt} = (K_p + K_{fm})M\lambda_0 = (1 + C_M)K_p M\lambda_0 = K_{pr}M\lambda_0 \quad (\text{A2})$$

$$\frac{dx_M}{dt} = (K_p + K_{fm})(1 - x_M)\lambda_0 = (1 + C_M)K_p(1 - x_M)\lambda_0 = K_{pr}(1 - x_M)\lambda_0 \quad (\text{A3})$$

Solvent

$$\frac{-1}{V_R} \frac{d(S.V_R)}{dt} = K_{fs}S\lambda_0 = C_S K_p S\lambda_0 = R_S K_{pr} S\lambda_0 \quad (\text{A4})$$

CTA

$$\frac{-1}{V_R} \frac{d(A.V_R)}{dt} = K_{fa}A\lambda_0 = C_A K_p A\lambda_0 = R_A K_{pr} A\lambda_0 \quad (\text{A5})$$

Live polymer chains length distribution based on Quasi Steady State Assumption (QSSA)

$$\frac{1}{V_R} \frac{d(\lambda_0.V_R)}{dt} = 2fK_d I - (K_{tc} + K_{td})\lambda_0^2 = 2fK_d I - K_t \lambda_0^2 \quad (\text{A6})$$

$$\begin{aligned} \frac{1}{V_R} \frac{d(\lambda_1 V_R)}{dt} &= 2fK_d I + K_p M \lambda_0 + (K_{fm} M + K_{fs} S + K_{fa} A)(\lambda_0 - \lambda_1) - (K_{tc} + K_{td}) \lambda_0 \lambda_1 \\ &2fK_d I + (M + R_S S + R_A A) K_{pr} \lambda_0 - K_t \lambda_0 \lambda_1 - (R_M M + R_S S + R_A A) K_{pr} \lambda_1 \\ &2fK_d I + (1 + R_{SM} + R_{AM}) K_{pr} M \lambda_0 - K_t \lambda_0 \lambda_1 - (R_{MM} + R_{SM} + R_{AM}) K_{pr} M \lambda_1 \end{aligned} \quad (A7)$$

$$\begin{aligned} \frac{1}{V_R} \frac{d(\lambda_2 V_R)}{dt} &= 2fK_d I + K_p M (2\lambda_1 + \lambda_0) + (K_{fm} M + K_{fs} S + K_{fa} A)(\lambda_0 - \lambda_2) - (K_{tc} + \\ &K_{td}) \lambda_0 \lambda_2 \\ &2fK_d I + (M + R_S S + R_A A) K_{pr} \lambda_0 + 2K_p M \lambda_1 - K_t \lambda_0 \lambda_2 - (R_M M + R_S S + R_A A) K_{pr} \lambda_2 \\ &2fK_d I + (1 + R_{SM} + R_{AM}) K_{pr} M \lambda_0 + 2K_p M \lambda_1 - K_t \lambda_0 \lambda_2 - (R_{MM} + R_{SM} + R_{AM}) K_{pr} M \lambda_2 \end{aligned} \quad (A8)$$

Dead polymer chain length distribution

$$\begin{aligned} \frac{1}{V_R} \frac{d(\mu_0 V_R)}{dt} &= (K_{fm} M + K_{fs} S + K_{fa} A) \lambda_0 + \left(K_{td} + \frac{K_{tc}}{2} \right) \lambda_0^2 \\ &(R_M M + R_S S + R_A A) K_{pr} \lambda_0 + \left(1 - \frac{R_T}{2} \right) K_t \lambda_0^2 \end{aligned} \quad (A9)$$

$$\begin{aligned} \frac{1}{V_R} \frac{d(\mu_1 V_R)}{dt} &= (K_{fm} M + K_{fs} S + K_{fa} A) \lambda_1 + (K_{td} + K_{tc}) \lambda_0 \lambda_1 \\ &(R_M M + R_S S + R_A A) K_{pr} \lambda_1 + K_t \lambda_0 \lambda_1 \end{aligned} \quad (A10)$$

$$\begin{aligned} \frac{1}{V_R} \frac{d(\mu_2 V_R)}{dt} &= (K_{fm} M + K_{fs} S + K_{fa} A) \lambda_2 + (K_{td} + K_{tc}) \lambda_0 \lambda_2 + K_{tc} \lambda_1^2 \\ &(R_M M + R_S S + R_A A) K_{pr} \lambda_2 + K_t \lambda_0 \lambda_2 + R_T K_t \lambda_1^2 \end{aligned} \quad (A11)$$

Energy balance equation

$$\frac{d(\rho \cdot C_p V_R T)}{dt} = (-\Delta H_p) K_p M \lambda_0 V_R - U A_H (T - T_{bath}) \quad (A12)$$

Volume variation with reaction

$$\frac{dV_R}{dt} = -\varepsilon V_{R0} \frac{dx_M}{dt} \quad (A13)$$

and

$$\text{Number average molecular weight } MW_n = \frac{\lambda_1 + \mu_1}{\lambda_0 + \mu_0} MW_M \approx \frac{\mu_1}{\mu_0} MW_M \quad (A14)$$

$$\text{Weight average molecular weight } MW_w = \frac{\lambda_2 + \mu_2}{\lambda_1 + \mu_1} MW_M \approx \frac{\mu_2}{\mu_1} MW_M \quad (A15)$$

$$\text{Polydispersity Index } PDI = \frac{MW_w}{MW_n} = \frac{(\lambda_2 + \mu_2)(\lambda_0 + \mu_0)}{(\lambda_1 + \mu_1)^2} \approx \frac{(\mu_2 \cdot \mu_0)}{(\mu_1)^2} \quad (\text{A16})$$

where

$$K_t = K_{tc} + K_{td} \quad (\text{A17})$$

$$K_{pr} = K_p + K_{fm} = (1 + C_M)K_p \quad (\text{A18})$$

$$C_M = \frac{K_{fm}}{K_p} \quad (\text{A19})$$

$$C_S = \frac{K_{fs}}{K_p} \quad (\text{A20})$$

$$C_A = \frac{K_{fa}}{K_p} \quad (\text{A21})$$

$$C_T = \frac{K_{td}}{K_{tc}} \quad (\text{A22})$$

$$R_T = \frac{K_{tc}}{K_{tc} + K_{td}} = \frac{K_{tc}}{K_t} = \frac{1}{1 + C_T} \quad (\text{A23})$$

$$R_M = R_{MM} = \frac{K_{fm}}{K_p + K_{fm}} = \frac{K_{fm}}{K_{pr}} = \frac{C_M}{1 + C_M} \quad (\text{A24})$$

$$R_S = \frac{C_S}{1 + C_M} = \frac{K_{fs}}{K_{pr}} \quad (\text{A25})$$

$$R_{SM} = \frac{C_S}{1 + C_M} \frac{S}{M} = R_S \cdot \frac{S}{M} \quad (\text{A26})$$

$$R_A = \frac{C_A}{1 + C_M} = \frac{K_{fa}}{K_{pr}} \quad (\text{A27})$$

$$R_{AM} = \frac{C_A}{1 + C_M} \frac{A}{M} = R_A \cdot \frac{A}{M} \quad (\text{A28})$$

$$R_P = R_{MM} + R_{SM} + R_{AM} = R_{MM} + R_{SA} \quad (\text{A29})$$

$$R_{SA} = R_{SM} + R_{AM} \quad (\text{A30})$$

$$\rho = \rho_M \Phi_M + \rho_P \Phi_P + \rho_S \Phi_S \quad (\text{A31})$$

$$Cp = Cp_M \Phi_M + Cp_P \Phi_P + Cp_S \Phi_S \quad (\text{A32})$$

$$\Phi_M = \frac{(1 - x_M)}{(1 - \varepsilon_0 x_M + \beta)} = \frac{(1 - x_M)}{(1 + \beta)(1 - \varepsilon x_M)} \quad (\text{A33})$$

$$\Phi_P = \frac{x_M(1 - \varepsilon)}{(1 - \varepsilon_0 x_M + \beta)} = \frac{x_M(1 - \varepsilon(1 + \beta))}{(1 + \beta)(1 - \varepsilon x_M)} \quad (\text{A34})$$

$$\Phi_S = \frac{\beta}{(1-\varepsilon_0 x_M + \beta)} = \frac{\beta}{(1+\beta)(1-\varepsilon x_M)} \quad (\text{A35})$$

$$V_R = V_{R0}(1 - \varepsilon \cdot x_M) \quad (\text{A36})$$

$$M = M_0 \frac{(1-x_M)}{(1-\varepsilon x_M)} \quad (\text{A37})$$

$$\varepsilon = \frac{\varepsilon_0}{1+\beta} \quad (\text{A38})$$

$$\varepsilon_0 = \frac{(\rho_P - \rho_M)}{\rho_P} = 1 - \frac{\rho_M}{\rho_P} \quad (\text{A39})$$

$$\beta = \frac{f_s}{(1-f_s)} \quad (\text{A40})$$

Meaning of all these symbols are same as commonly used and can be found in notation section.

Appendix-B: Zhu Transformation and New transformation.

Zhu transformation is as follows

$$\text{For initiator, } I' = \frac{I}{I_0} \quad (\text{B1})$$

$$\text{For monomer, } M' = \frac{M}{M_0} \quad (\text{B2})$$

$$\text{For solvent, } S' = \frac{S}{S_0} \quad (\text{B3})$$

$$\text{For CTA, } A' = \frac{A}{A_0} \quad (\text{B4})$$

$$\mu'_0 = \frac{\mu_0}{I_0} \quad (\text{B5})$$

$$\mu'_1 = \frac{\mu_1}{M_0} \quad (\text{B6})$$

$$\mu'_2 = \frac{\mu_2}{(M_0^2/I_0)} \quad (\text{B7})$$

To apply NT, as developed in our previous work,⁹ following assumptions are required:

1. Quasi-steady state assumption (QSSA) for live polymer radicals chain lengths distributions $\lambda_0, \lambda_1, \lambda_2$ to eqs (A6)-(A8), we obtained:

$$\lambda_0 = \sqrt{\frac{2fK_dI}{(K_{tc}+K_{td})}} = \sqrt{\frac{2fK_dI}{K_t}} \quad (\text{B8})$$

$$\lambda_1 = \lambda_0(\dot{L} + 1) \quad (\text{B9})$$

$$\lambda_2 = \lambda_1(2\dot{L} + 1) = \lambda_0(\dot{L} + 1)(2\dot{L} + 1) \quad (\text{B10})$$

where

$$\dot{L} = L \cdot \left(\frac{1-R_{MM}}{1+R_{PL}} \right) = L \cdot \left(\frac{1-R_M}{1+R_{PL}} \right) \quad (\text{B11})$$

$$L = \frac{(K_p+K_{fm})M\lambda_0}{2fK_dI} = \frac{K_{pr}M\lambda_0}{2fK_dI} \quad (\text{B12})$$

2. For $\dot{L} \gg 1$

$$\lambda_1 = \lambda_0\dot{L} \quad (\text{B13})$$

$$\lambda_2 = 2\dot{L}\lambda_1 = 2\dot{L}^2\lambda_0 \quad (\text{B14})$$

The NT for kinetic rate coefficients is as follows:

$$\text{For dissociation: } K'_d = K_d \quad (\text{B15})$$

$$\text{For propagation: } K'_p = K_p \sqrt{I_0 \cdot M_0} \quad (\text{B16})$$

$$\text{For termination: } K'_t = K_t M_0 \quad (\text{B17})$$

So eqs. (B15) - (B17) constitutes the NTs where all terms marked with (') are dimensionless in terms of concentration. K_d does not require any transformation as it is already dimensionless in terms of concentration. All the transfer rate coefficients like transfer to monomer K_{fm} , transfer to solvent K_{fs} , and transfer to CTA K_{fa} are connected to K_p through eq. (A18) to (A21) and (A24) to (A28) in Appendix-A. Similarly, K_t is connected to $K_{tc} \wedge K_{td}$ through eq. (A17), (A22) & (A23) in Appendix-A. An additional relationship for eq. A29 is required if any of the transfer processes is/are involved which is as follows:

$$R'_p = R_p \cdot \frac{M_0}{I_0} \quad (\text{B18})$$

Applying NT results into the following relationships between their dimensionless and dimensional forms:

$$\lambda'_0 = \sqrt{\frac{2fK'_d I'}{K'_t}} = \frac{\sqrt{\frac{2fK_d I}{K_t} * 1}}{\sqrt{I_0 M_0}} = \frac{\lambda_0}{\sqrt{I_0 M_0}} \quad (\text{B19})$$

$$L' = \frac{K'_p \lambda'_0 M'}{2fK'_d I'} = \frac{K_p \lambda_0 M}{2fK_d I} * \left(\frac{I_0}{M_0}\right) = L \left(\frac{I_0}{M_0}\right) \quad (\text{B20})$$

$$\acute{L}' = L' \cdot \left(\frac{1-R'_{MM}}{1+R'_p L'}\right) = L \cdot \left(\frac{1-R_M}{1+R_p L}\right) = \acute{L} \quad (\text{B21})$$

$$DPn = \frac{\mu_1}{\mu_0} = \frac{\mu'_1}{\mu'_0} \left(\frac{M_0}{I_0}\right) \quad (\text{B22})$$

$$PDI = \frac{\mu_0 \mu_2}{\mu_1^2} = \frac{\mu'_0 \mu'_2}{\mu_1'^2} \quad (\text{B23})$$

Appendix-C: Expression for the variations in viscosity, density and thermal conductivity for MMA.

Viscosity

$$c_p = 1.2\Phi_p \quad (C1)$$

$$f_v = [0.025 + 10^{-3}(T(^{\circ}C) + 106)]\Phi_m + [0.025 + 10^{-3}(T(^{\circ}C) + 180)]\Phi_s + [0.025 + 0.48 \times 10^{-3}(T(^{\circ}C) - 114)]\Phi_p \quad (C2)$$

$$\eta_m = \exp \left[2.303 \left(\frac{0.115}{0.025 + 10^{-3}(T(^{\circ}C) + 106)} - 1 \right) \right] \quad (C3)$$

$$\eta = \eta_m + 0.6c_p^{1.4} \exp \left(\frac{0.8}{f_v} \right) \text{ for } c_p < 0.13 \text{ g/cm}^3 \quad (C4)$$

$$\eta = \eta_m + 200c_p^{4.2} \exp \left(\frac{0.8}{f_v} \right) \text{ for } c_p > 0.13 \text{ g/cm}^3 \quad (C5)$$

where Φ_m, Φ_p, Φ_s are volume fraction of monomer, polymer and solvent defined by eqn.(A33)-(A35) respectively, η the viscosity is in centipoise, f_v the fractional free volume, c_p the polymer concentration in g/cm^3 and η_m a parameter.

Density

$$\rho = \rho_M\Phi_M + \rho_P\Phi_P + \rho_S\Phi_S \quad (A31)$$

$$\rho_M \left(\frac{\text{g}}{\text{cm}^3} \right) = 0.968 - 1.225 \times 10^{-3}(T - 293.15) \quad (C6)$$

$$\rho_P \left(\frac{\text{g}}{\text{cm}^3} \right) = 1.212 - 8.45 \times 10^{-4}(T - 273.15) \quad (C7)$$

$$\rho_S \left(\frac{\text{g}}{\text{cm}^3} \right) = 0.883 - 9 \times 10^{-4}(T - 273.15) \quad (C8)$$

where ρ_M, ρ_P, ρ_S are density of monomer, polymer and solvent respectively.

Thermal Conductivity

$$k \left(\frac{W}{m.K} \right) = k_m w_m + k_s w_s + k_p w_p \quad (C9)$$

$$k_m = \frac{418.6 \times 47.61}{(T(^{\circ}C) + 273.15)} \times \left[\frac{0.9665 - 0.0011T(^{\circ}C)}{100.12} \right]^{\frac{4}{3}} \quad (C10)$$

$$k_s = \frac{418.6 \times 66.70}{(T(^{\circ}C) + 273.15)} \left[\frac{0.8838 - 0.00087T(^{\circ}C)}{92.14} \right]^{\frac{4}{3}} \quad (C11)$$

$$k_p = 418.6 \times 4.5 \times 10^{-4} \quad (C12)$$

where $w_m, w_s, \wedge w_p$ are weight fractions of monomer, solvent and polymer respectively, given by following expressions:

$$w_m = \frac{1 - x_m}{1 + \beta} \quad (C13)$$

$$w_s = \frac{\beta}{1 + \beta} \quad (C14)$$

$$w_p = \frac{x_m}{1 + \beta} \quad (C15)$$

where β is given by eqn. (A40).

Appendix-D: Visualizing mixing inside the three tubular microreactors using mass-less tracer particles

For visualizing the impact of variation in density and viscosity on flow profile inside the reactor, a mass-less tracer particles technique as available in CFD-VIEW was used. These particles were numerically injected at various positions uniformly spaced at the inlet cross-section. The results are presented for STR, CTR and CFIR in **Figures 11 to 17**.

In **Figure 11**, on x-axis, chordlength represented the distance along the flow from the reactor inlet. y-axis represented velocity magnitude of the individual tracer particle at different x , i.e. different distances along the flow inside reactor. Different velocities for different particles at $x = 0$, were due to parabolic velocity profile (fully developed flow) imposed at inlet. It could easily be seen that for constant FPHP case, the particles followed straight streamlines as expected. For variable FPHP case, the streamlines bended due to the variation in density and viscosity as shown in **Figure 12**. This bending of streamlines occurred because of following reason. As soon as the monomer-initiator solution entered the STR, reaction started. But the residence time was higher near the wall due to no-slip boundary condition. This led to higher conversion near the wall. Thus viscosity and density increased more near the wall. This constricted the flow through the cross section. This caused deceleration for the flow near the wall and acceleration for the central flow initially. Meanwhile at the central region of the flow, the reaction mixture experienced a lower residence time and hence lower conversion. Consequently, the viscosity was low initially but as it experienced more residence time, conversion increased and thus viscosity and density also increased. This led to its deceleration. But still there was no radial mixing due to convective process as no particle crosses each other's path.

This was not the case for CTR and CFIR. In **Figure 13** for CTR, the velocity profiles for various particles along the flow were quite random for both constant and variable FPHP cases because of the secondary flow induced due to curvature. After certain length along the flow, the velocity

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

profile for all the particles fluctuated within a smaller range for constant FTPP (decoupled transport processes) case. This range of fluctuation along with fluctuation got further narrowed down for variable FTPP (coupled transport processes) case. The streamlines of the tracer particles at the outlet could be seen in **Figure 14**.

Different velocity profiles were obtained for different values of the diffusion coefficient. This could be explained as follows. Different values of conversions at outlet were achieved for different values of diffusion coefficients and thus different values of viscosities and densities were spatially observed along the flow. Due to no-slip boundary condition at the wall, the residence time was higher near the wall leading to higher conversion. This increased viscosity near the wall. Along the flow, this envelop of high viscosity expanded towards the center of the tube from the wall. Thus the area available for the low-viscosity flow was reduced along the flow. This could be observed in **Figure 14 (b)** and **Figure 14 (c)**. The same observation was made by Baillagou et al.^[5] too. No particle in this simulation reached zero velocity, hence it could be deduced that no particle reached the wall for the constant FTPP case where the velocity should be equal to zero because of no-slip condition. Since these particles were modeled as massless tracer particles, if they reached the wall and attained zero velocity, they could not move further as the simulation was steady state. The interpretation of this situation in physical terms is as follows. These tracer particles would represent volume packets in real flow. So, if these tracer particles would reach the wall, it would mean that the volume packets with different residence times would reach the wall. Once they reached the wall, they would need to replace stagnant volume packets from there near the wall and in this process would attain zero velocity themselves. Thus, this process would bring volume packets with higher residence time to mainstream. Hence, this would improve radial mixing and would narrow down the residence time distribution. For the case of constant FTPP case, **Figure 14 (a)** shows no tracer particle reaching zero velocity. But for variable FTPP case, a few tracer particles did reach zero velocity in the beginning when viscosity was low as shown in **Figure 14 (b)**. At later stage, both **Figure**

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

14 (b) and (c) show not much radial mixing. Thus, variable FTPP modeling predicted more radial mixing in CTR compared to constant FTPP case which was closer to reality. However, both types of modeling predicted a relatively poor radial mixing overall in CTR.

For CFIR as shown in **Figure 15**, the results were quite different compared to CTR. CFIR was designed to be a chaotic device.^[12] The chaos being introduced by the 90° bend at regular intervals as shown in **Figure 1**. The lead to chaotic advection^[27-29] as explained later. So, despite having the same injection location at the inlet as in CTR, the velocity profiles for different massless tracer particles along the flow was totally different. Each bend changed the velocity profile despite such a low inlet Reynolds number which decreased further along the path in variable FTPP case (due to increase in viscosity). This was quite remarkable from the fact that due to this phenomenon, even at such a low Reynolds number and thus low Dean number, more tracer particles compared to CTR reached the wall starting from first to second bend itself. This indicated better radial mixing capability of CFIR. Because of this, only some of the injected particles reached the reactor outlet as could be seen in **Figure 16**. This indicated better radial mixing capability of CFIR compared to CTR and STR under similar operating conditions. The number of particles reaching outlet decreased for the lower value of diffusion coefficient and increased for the higher value of diffusion coefficient in both coupled and decoupled transport processes case.

In chaotic advection, two particles, even if they were very close to each other at the beginning, when start moving along the flow followed totally different paths ultimately. i.e. they could not be traced back to their original starting positions. This has been shown in **Figure 17** for both constant and variable FTPP cases. Generally chaotic advection is obtained for unsteady state flow but in our case it was observed even in steady state case. This is consistent with the published results that a non-viscous steady-state 3D flow could be chaotic^[27] under certain conditions. The whole region of flow might not have chaotic advection depending upon operating conditions. For non-chaotic region of flow, the two massless tracer particles placed

1 very near to each other would follow the similar paths and hence would have the same velocity
2 profile. Chaotic advection, thus, could be observed only at certain points of entry to inlet. In
3
4 **Figure 17**, the first column shows the injection location of the tracer particles at inlet whereas
5
6 the second column showed the velocity profiles of particles along the path. **Figure 17(a)** shows
7
8 that the two tracer particles reaching the wall at two different distances for the constant FTPP
9
10 case. In **Figure 17(b)**, one of the particles reached the wall while other reached the outlet
11
12 showing the chaotic advection. Same result was observed for variable FTPP case in **Figure**
13
14 **17(c)**. As could be seen that the velocity profiles for both the tracer particles remained nearly
15
16 same for some length along the flow initially. But after first bend and second bend, the profiles
17
18 changes completely indicating chaos.
19
20
21
22

23
24 [27] H. Aref, *J Fluid Mech*, **1984**, 143 (Jun), 1.

25
26 [28] H. Aref, *Philos T Roy Soc A*, **1990**, 333 (1631), 273.

27
28 [29] H. Aref, *Phys Fluids*, **2002**, 14 (4), 1315.
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65

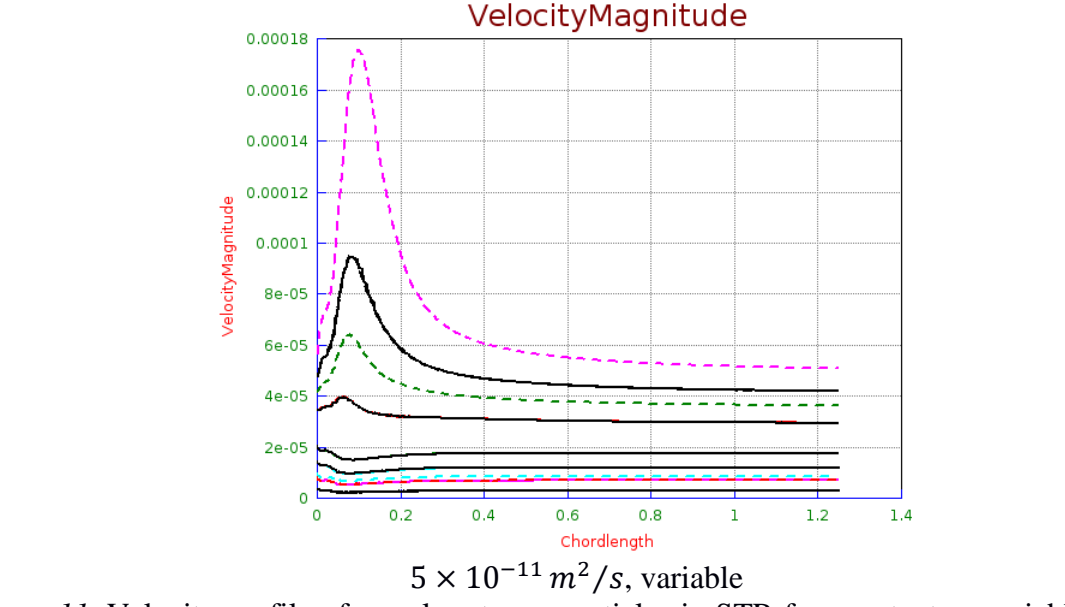
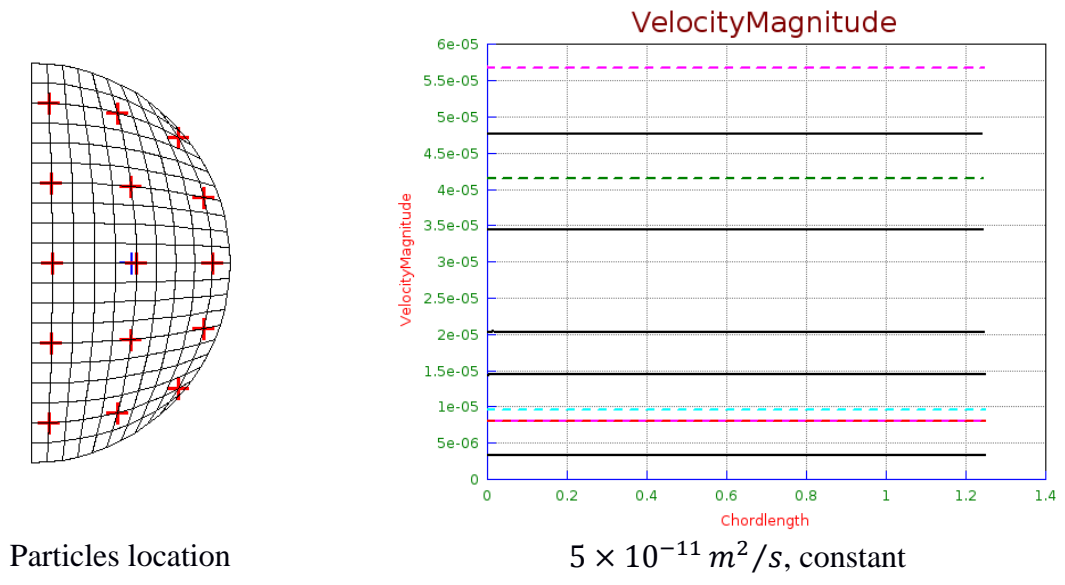


Figure 11. Velocity profile of massless tracer particles in STR for constant or variable FTPP and at a given value of diffusion coefficient

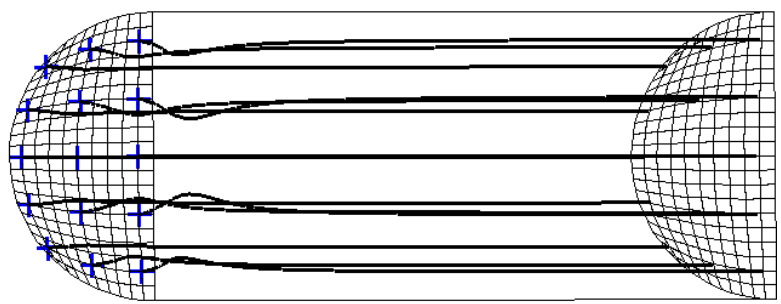
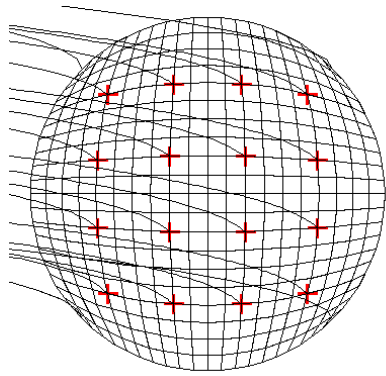
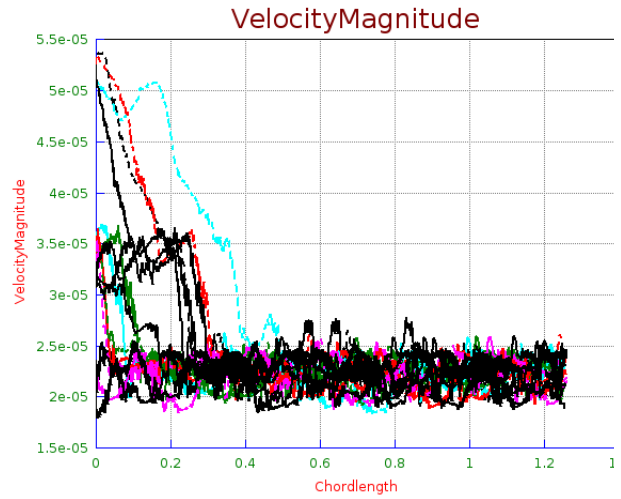


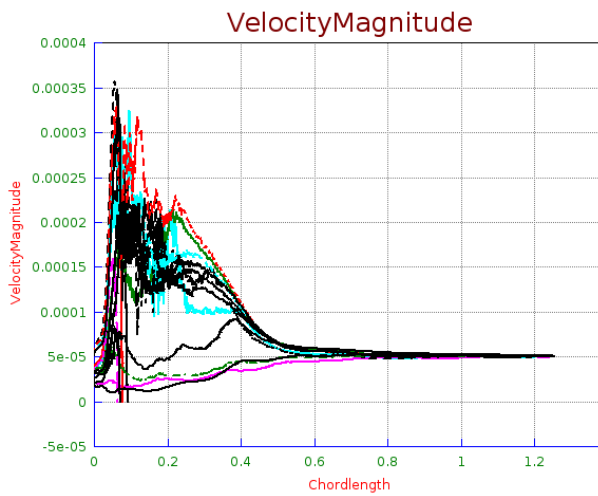
Figure 12. Streamlines of tracers in STR variable FTPP (left is inlet with blue dots for tracers origin and right is outlet of STR)



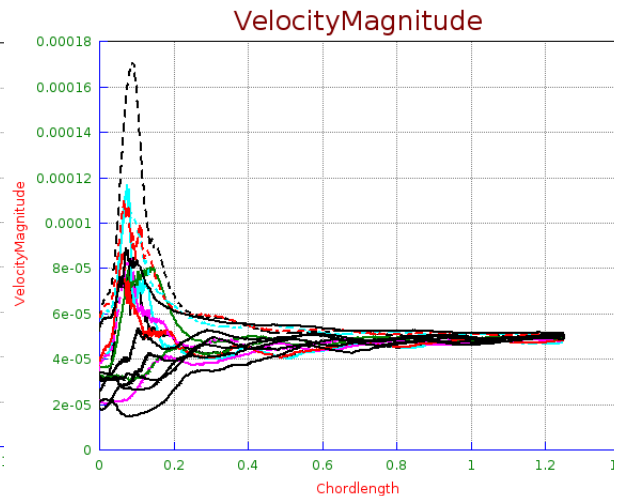
Particles location



$5 \times 10^{-11} \text{ m}^2/\text{s}$, constant



$5 \times 10^{-11} \text{ m}^2/\text{s}$, variable



$1 \times 10^{-10} \text{ m}^2/\text{s}$, variable

Figure 13. Velocity profile of massless tracer particles in CTR for constant or variable FTPP and at two different values of diffusion coefficient

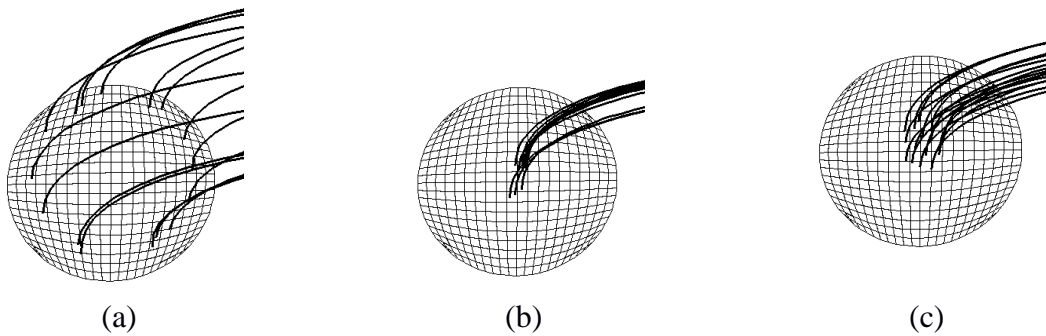
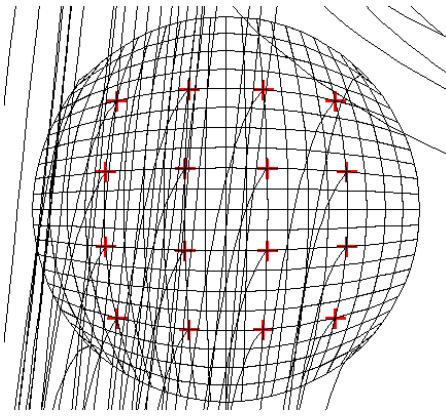
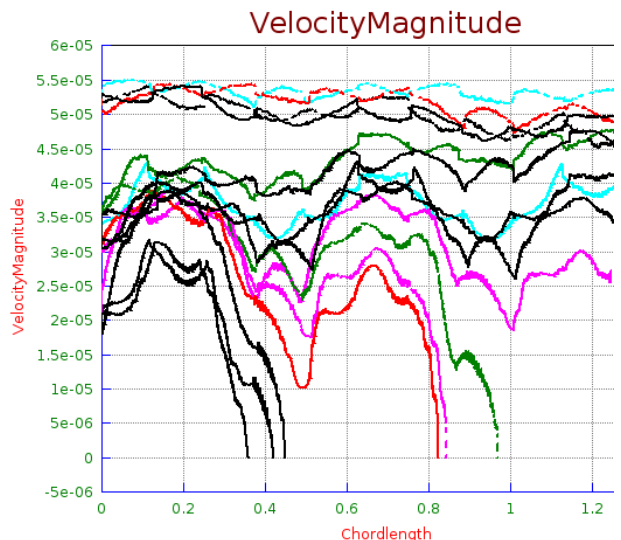


Figure 14. Streamlines of tracers at CTR outlet for a) constant, b) variable fluid property cases at $D = 5 \times 10^{-11} \text{ (m}^2/\text{s)}$, and c) $D = 1 \times 10^{-10} \text{ (m}^2/\text{s)}$.

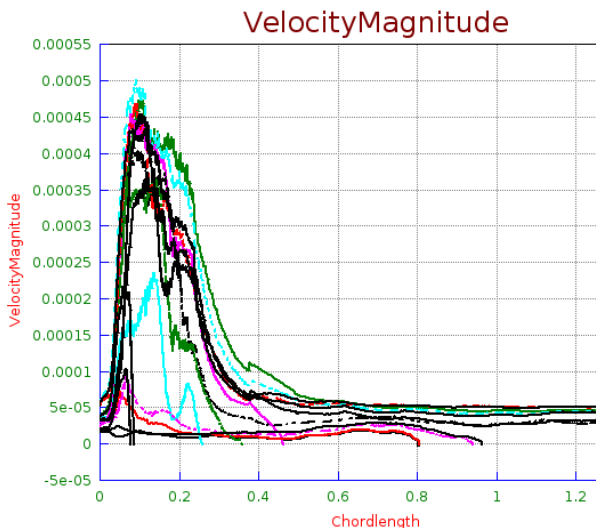
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65



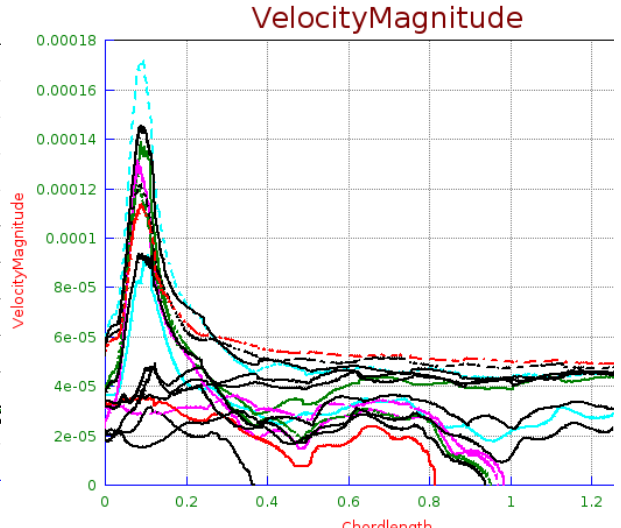
Particles location



$5 \times 10^{-11} \text{ m}^2/\text{s}$, constant



$5 \times 10^{-11} \text{ m}^2/\text{s}$, variable



$1 \times 10^{-10} \text{ m}^2/\text{s}$, variable

Figure 15. Velocity profile of massless tracer particles in CFIR for constant or variable FTPP and at two different values of diffusion coefficient

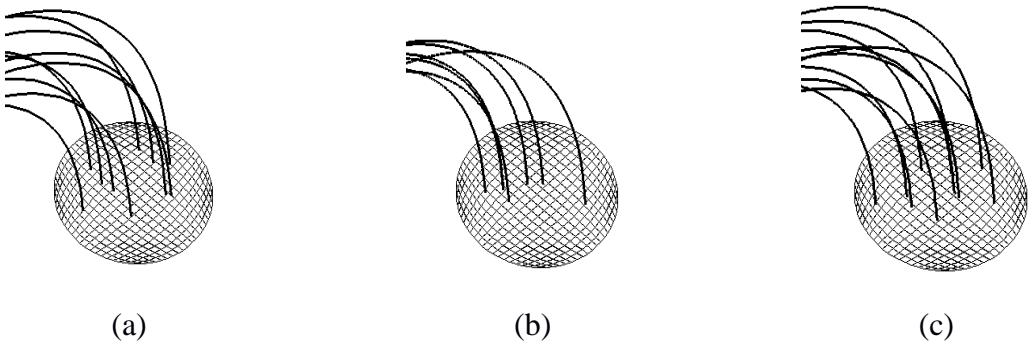
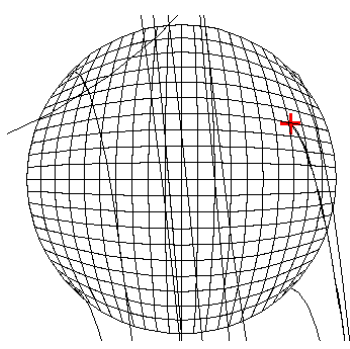
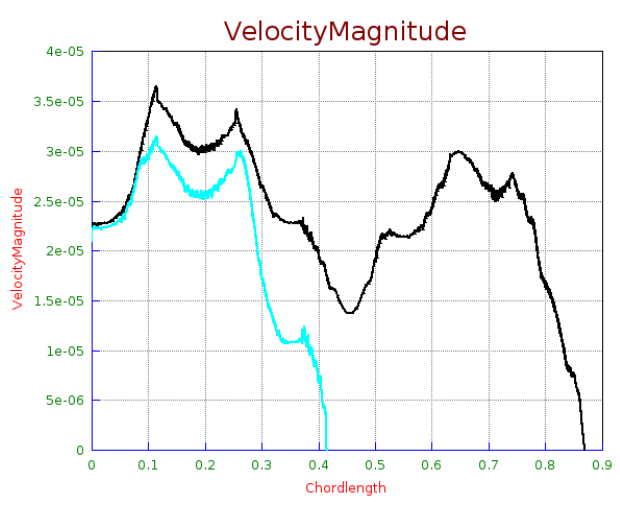


Figure 16. Streamlines of tracers at CFIR outlet for a) constant, b) variable fluid property cases at $D = 5 \times 10^{-11} \left(\frac{\text{m}^2}{\text{s}}\right)$, and c) $D = 1 \times 10^{-10} \left(\frac{\text{m}^2}{\text{s}}\right)$

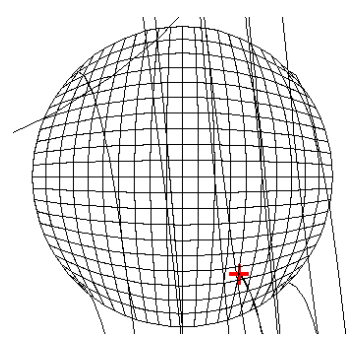
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65



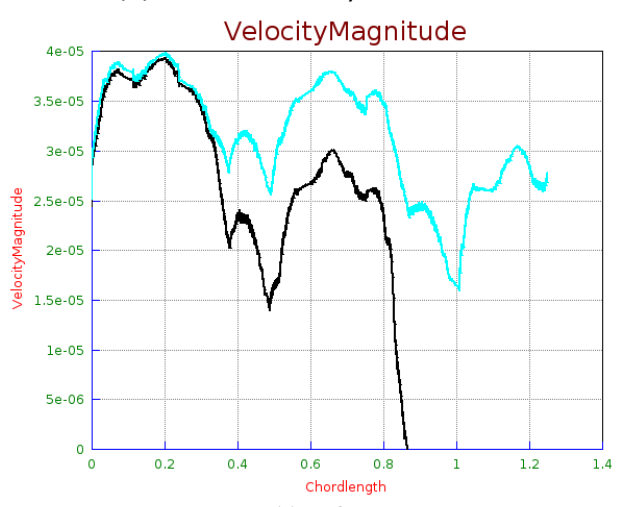
Particles location



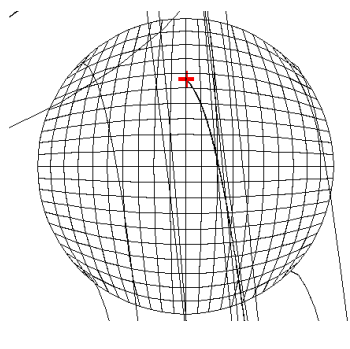
(a) $5 \times 10^{-11} \text{ m}^2/\text{s}$, constant



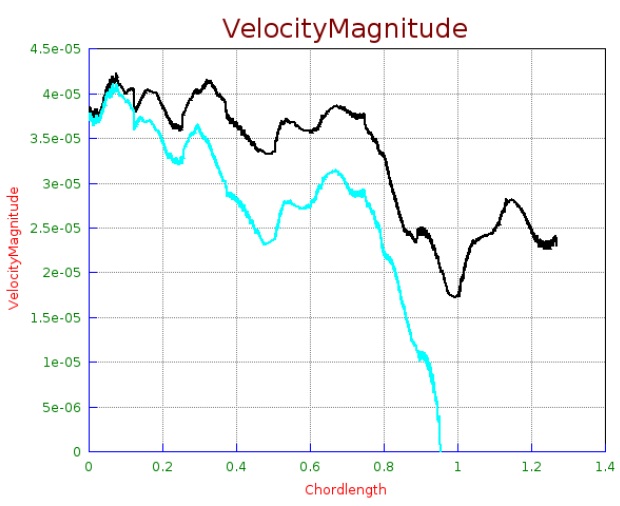
Particles location



(b) $5 \times 10^{-11} \text{ m}^2/\text{s}$, constant




Particles location



(c) $5 \times 10^{-11} \text{ m}^2/\text{s}$, variable

Figure 17. Results showing chaotic trend for two nearly spaced particles at CFIR inlet



Click here to access/download

Production Data

Garg_MacroT&S2_Masucrypt_Major_Revision_1.pdf

